

Fully Documented Version of the Algorithm `arrayMax`

A (reasonably) fully documented version of the algorithm `arrayMax` — including the precondition and postcondition for the problem being solved, loop invariant and bound function for the `while` loop in this algorithm, and various other assertions that help to document a proof of the correctness of this algorithm, is as follows.

```
// Precondition: An integer array A, with some positive length n, is given as input.
// Postcondition: The largest element in the set
//                 {A[0], A[1], ..., A[n - 1]}
//                 is returned as output.
integer arrayMax ( integer[] A ) {
    // Assertion: A is an input integer array with some positive length n.
    1. if (A.length == 1) {
        // Assertion: A is an input integer array with length n = 1.
        2. return A[0]
        // Assertion:
        // 1. A is an input integer array with length n = 1.
        // 2. The largest element in the set
        //     {A[0], A[1], ..., A[n - 1]} = {A[0]}
        //     has been returned as output.
    } else {
        // Assertion: A is an integer array with length n ≥ 2.
        3. integer i := 0
        4. integer maxSoFar := A[0]
        // Loop Invariant:
        // 1. A is an input integer array with some length n such that n ≥ 2.
        // 2. i is an integer variable such that 0 ≤ i ≤ n - 1.
        // 3. maxSoFar is an integer variable such that
        //     maxSoFar = max(A[0], A[1], ..., A[i]).
        // Bound Function: n - i, that is, A.length - i
    }
}
```

```

// Assertion:
// 1. The loop invariant for this while loop is satisfied.
// 2.  $i = 0$ .
5. while ( $i < A.length - 1$ ) {
    // Assertion:
    // 1. The loop invariant for this while loop is satisfied.
    // 2.  $0 \leq i \leq A.length - 2$ 
6.      $i := i + 1$ 
7.     if ( $maxSoFar < A[i]$ ) {
8.          $maxSoFar := A[i]$ 
    }
    // Assertion: The loop invariant for this while loop is satisfied.
}
// Assertion:
// 1. The loop invariant for this while loop is satisfied.
// 2.  $i = A.length - 1$ 
9. return  $maxSoFar$ 
// Assertion:
// 1. A is an input integer array with some length  $n$  such that  $n \geq 2$ .
// 2. The largest element in the set
//          $\{A[0], A[1], \dots, A[n - 1]\}$ 
//     has been returned as output.
}
// Assertion:
// 1. A is an input integer array with some positive length  $n$ .
// 2. The largest element in the set
//          $\{A[0], A[1], \dots, A[n - 1]\}$ 
//     has been returned as output.
}

```