

# Secure Optimization of Inlined Reference Monitors

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## Abstract

Inlined Reference Monitor (IRM) is the preferred enforcement mechanism for history-based access control policies. IRM enforcement injects monitoring code into the binary of an untrusted program in order to track its execution history. The injected code denies access when execution deviates from the policy. The viability of IRM enforcement is predicated on the ability of the binary rewriting element to optimize away redundant monitoring code without compromising security.

This work proposes a novel optimization framework for IRM enforcement. The scheme is based on a constrained representation of history-based access control policies, which, despite its constrained expressiveness, can express such policies as separation of duty, generalized Chinese Wall policies, and hierarchical one-out-of- $k$  authorization. An IRM optimization procedure has been designed to exploit the structure of this policy representation. The optimization scheme is then extended into a distributed optimization protocol, in which an untrusted code producer attempts to help boost the optimization effectiveness of an IRM enforcement mechanism administered by a distrusting code consumer. It is shown that the optimization procedure provably preserves security even in the midst of distributed optimization. A prototype of the optimization procedure has been implemented for Java bytecode, and its effectiveness has been empirically profiled.

**Keywords:** Language-based security, history-based access control policies, inlined reference monitors, security automata, distributed optimization protocol.

## 1 Introduction

This paper presents novel implementation techniques for the protection mechanism of extensible systems, that is, software systems composed of a trusted application core collaborating with a number of untrusted software components, all running within the same address space. To support the late binding of features to an application, the latter could be made extensible by adopting a

plug-in architecture or offering scripting support. This paper focuses on language-based extensible systems [32] such as those developed on the safe language environments Java and .Net. In these systems, untrusted components collaborate with the application core through a well-defined Application Programming Interface (API). To protect the integrity of the resources encapsulated by the API, it is in the interest of the application core to ensure that access requests made by the untrusted components through the API honor certain security policies. A notable such family of security policies are history-based access control policies, in which an authorization decision is made solely on the basis of the execution history of the target program as observed by the enforcement mechanism at run time [13, 33, 21, 22]. Such policies are safety properties [33]. Examples include the Chinese Wall policy [9], Biba’s low water mark policy [7], one-out-of- $k$  authorization [13], assured pipelines [8], as well as Stack Inspection [41] and its variants [1].

Execution monitoring [13, 14, 42] is the standard enforcement mechanism for history-based access control policies. The classical implementation strategy is to interpose a reference monitor at the entry points of the API, so that the monitor may track the API calls previously made, arguments passed, or even the run-time state of the untrusted component to ensure policy compliance. This is the implementation strategy adopted by the Java platform in its Stack Inspection mechanism [17]. A modern implementation strategy for execution monitoring is Inlined Reference Monitor (IRM) [39], in which monitoring code is injected into an untrusted component through binary rewriting. The advantage of IRM over interpositioning is that IRM fully decouples the enforcement mechanism from the application core, thereby allowing the security model to evolve separately from the application code base. An important challenge faced by IRM enforcement mechanisms is the run-time overhead induced by the injected code [41, 33]. Viability of the IRM approach is predicated on the ability of the binary rewriting element to optimize away unnecessary monitoring code [11].

In this work, we explore the interplay between security concerns and optimization procedures for IRM enforcement of history-based access control policies. Our contribution is twofold:

1. **Optimization-friendly policy representation:** Since [33, 38, 39], the Security Automaton has become the standard representation for security policies to be enforced by execution monitoring. A research concern [5, 16, 23, 36, 37] of the language-based security community has been the following: Can we trade off the expressiveness of policy representation (i.e., by adopting a less powerful version of the Security Automaton) for improved resource consumption (e.g., time, space, information) of the execution monitor? In this work, we address a related but novel research question: *Can we trade off the expressiveness of policy representation for improved effectiveness of the optimization element in the IRM binary rewriter?* By adopting a declarative state representation and imposing structures on state transitions, we have shown that one can employ standard compiler optimization techniques to optimize away state transition code that would otherwise be injected into the target program, and do so without compromising security. We also demonstrate that the resulting policy representation is still expressive enough to encode a wide range of history-based access control policies.
2. **Distributed optimization protocol:** To further enhance the effectiveness of IRM optimization, we propose a distributed optimization protocol that has been inspired by Proof-Carrying Code [27]. Specifically, an untrusted code producer sends a software component to a distrusting code consumer for execution. To promote usage of the component, the code producer ships a version of the component that has been annotated with optimization directives,

which are hints on how the code consumer can aggressively optimize the monitor code to be injected into the component for IRM enforcement. As the code producer could very well be malicious, blindly following the optimization directives could lead to the omission of key monitoring logic, thus compromising security. To counter this, the code consumer injects into the component specially designed run-time checks that will be completely optimized away if the code producer is honest about the optimization directives, but will detect the dishonesty at run time if the code producer attempts to mislead the code consumer.

The rest of this paper outlines the proposed policy representation (Section 3), the optimization procedure that takes advantage of this policy representation (Section 4), a corresponding distributed optimization protocol (Section 5), extensions to support Java-style language constructs (Section 6), as well as an implementation (Section 7) and its empirical evaluation (Section 8).

## 2 Related Work

What we call history-based access control policies are safety properties. Schneider characterized the security policies enforceable by execution monitoring to be safety properties [33], and proposed Security Automata (SA) as the standard representation of execution monitors. (A recent sharpening of this result can be found in [18].) Inlined Reference Monitoring was first proposed in [39] as a framework to unify previous work [13, 14] that employs binary rewriting to enforce history-based access control policies. Fong proposed an information-based characterization of security policies enforceable by execution monitors consuming only a limited portion of history information [16]. The goal was to understand the trade-off between the differentiating power of an execution monitor and the resource to which it is made available, a goal first articulated by Ligatti *et al* [5, 23]. The work has been refined by Talhi *et al* to obtain a characterization of execution monitors operating under memory constraints [36, 37]. Our work poses a related but novel question: can the expressiveness of policy representation be restricted to facilitate IRM optimization? Our policy representation is formally akin to STRIPS planning operators [15].

A first principled design of optimization procedures for IRM enforcement mechanisms is [11], which assumes each transition has a constant cost. Our optimization procedure is designed for unbounded state space, and thus we adopted a different performance metric (see Section 4). As IRM enforcement could be seen as a special-case of Aspect-Oriented Programming (AOP) [20], previous work on optimization techniques for AOP languages (e.g., [4]) is also relevant. Our work is unique in that we facilitate optimization by trading off policy expressiveness and by adopting a distributed optimization protocol.

Proof-Carrying Code (PCC) [27] pioneered the idea of self-certifying code. Specifically, a proof of safety is shipped along with an untrusted program, allowing the code consumer to verify safety in a tractable manner. Rose and Rose proposed a lightweight Java bytecode verification framework [30], in which type states are shipped along with Java classfiles, so that bytecode verification can be performed more efficiently. In model-carrying code [34], the code producer ships an untrusted program together with its behavior model. The model is checked by the code consumer against a preset policy for compliance. The verified model is then employed to monitor the execution of the untrusted program. In [2], a PCC-style safety proof is attached to an untrusted program to certify that an execution monitor has been properly inlined. Compared to the work above, ours

```

manager();
if (...) {
    accountant();
}
if (...) {
    critical();
    manager();
}
accountant();
critical();

```

(a) Original program

Program Point	Event
after manager()	<i>m</i>
after accountant()	<i>a</i>
before critical()	<i>c</i>

(b) Event interpretation

```

bool pm = false;
bool pa = false;
manager();
pm = true;
if (...) {
    accountant();
    pa = true;
}
if (...) {
    if (pm ∧ pa) { pm = false; pa = false; }
    else throw new IRMException();
    critical();
    manager();
    pm = true;
}
accountant();
pa = true;
if (pm ∧ pa) { pm = false; pa = false; }
else throw new IRMException();
critical();

```

(c) Execution monitor is inlined

Figure 1: IRM Enforcement of Separation of Duty

is unique in that we are the first to propose annotations for facilitating IRM optimization rather than verification.

CMV [35] is a model checker for verifying complete mediation [31] in the Stack Inspection enforcement mechanism of a Java Virtual Machine (JVM) implementation. Our work could be seen as a generalization of the static analysis performed by CMV to (1) support a more general class of safety properties and (2) inject dynamic checks when a target property cannot be statically verified. Both systems employ a notion of method interfaces (called method summaries in [35]) to modularize analysis. While method summaries are computed by a special-purpose algorithm, method interfaces are generated by a work-list-based whole-program analysis (Appendix C).

### 3 An Optimization-Friendly Policy Representation

**Notations** Given a record  $r$  with schema  $\langle f_1, \dots, f_k \rangle$ , we refer to the  $f_i$  component of  $r$  by the notation  $r.f_i$ . Thus, if  $o$  is an instance of the schema  $\langle pre, eff \rangle$ , then  $o.pre$  refers to the first component of  $o$ .

#### 3.1 Inlined Reference Monitor

Consider the enforcement of Separation of Duty [10] in an example program shown in Figure 1 (a) (adapted from [11], in turn inspired by [19, 6]). Our goal is to ensure that the operation `critical()` is performed only under the endorsement of both the operations `manager()` and

accountant(). To precisely articulate this policy, we interpret<sup>1</sup> the run-time traversal of certain program points to be security-relevant events (Figure 1 (b)): events  $m$ ,  $a$  and  $c$  correspond respectively to the three operations. Program execution therefore generates an event sequence. For example, if both of the “then” branches are executed, then the event sequence  $macmac$  will be generated. On the other hand, if the first “then” branch is not executed, then the sequence will be  $mcmac$ . Our Separation of Duty policy can then be phrased as a safety property regarding the generated event sequences [33]. For instance,  $macmac$  satisfies the policy, but  $mcmac$  does not. One way to enforce such a policy is through Inlined Reference Monitors (IRMs) [39]. Specifically, monitoring code is injected into the program points of interest, tracking the history of execution, and aborting execution whenever a policy violation is detected. In Figure 1 (c), monitoring code has been injected into the original programs identified in Figure 1 (b), tracking the occurrences of events  $m$  and  $a$ , and ensuring that every occurrence of event  $c$  is properly guarded.

Since [33, 38, 39], history-based access control policies are represented by Security Automata. A *Security Automaton (SA)* is a quadruple  $M = \langle \Sigma, Q, q_0, \{\delta_a\}_{a \in \Sigma} \rangle$ , where

- $\Sigma$  is a countable set of *access events*,
- $Q$  is a countable set of *monitor states*,
- $q_0 \in Q$  is a distinguished *start state*, and
- $\{\delta_a\}_{a \in \Sigma}$  is a family of *transition functions*, indexed by access events, such that each transition function  $\delta_a : Q \rightarrow Q$  is a partial function mapping the current monitor state to an optional next state.

Given an event sequence  $w \in \Sigma^*$ , we write  $\delta_w$  for the partial function defined inductively as follows:  $\delta_\epsilon = \iota_Q$ , the total identity function for  $Q$ , and  $\delta_{a \cdot w} = \delta_w \circ \delta_a$  (i.e., function composition). Note that, since  $\delta_w$  is partial,  $\delta_w(q)$  may not be defined for every state  $q$ . An event sequence  $w \in \Sigma^*$  is considered policy compliant iff  $\delta_w(q_0)$  is defined.

At the program points corresponding to event  $a$ , IRM injects a code fragment that simulates  $\delta_a$ . The inlining of such code fragments causes degradation of execution efficiency. A competitive IRM implementation will subject these code fragments to aggressive optimization.

## 3.2 A Constrained Policy Representation

Any practical policy representation must place constraints on the  $Q$  and  $\delta$  components [38, 39, 3]. We consider representation constraints that facilitate IRM optimization. Our proposed policy representation is based on two design choices that balance efficiency considerations against policy expressiveness.

**Design choice 1: Unbounded state space, finitary transitions** Unlike [11], which assumes  $Q$  to be finite, we anticipate the state space to be unbounded for practical IRM. Specifically, we envision the employment of IRM rewriting at load time, such that the state space may have to be expanded

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<sup>1</sup>Such an interpretation could have been induced by a protection mechanism built into the software deployment environment, a software certification process, or an aspect-oriented programming system [20]. Our work can be applied to each of these contexts.

when new code units are dynamically loaded. It is therefore assumed that each application domain is associated with a *countable* set  $\Pi$  of propositional variables<sup>2</sup>, called *state variables*. A  $\Pi$ -state, or simply a state, is an assignment of truth values to propositional variables from  $\Pi$ , such that the assignment differs from one of the following three truth assignments for only finitely many propositional variables: (i) all propositions are undefined, (ii) all propositions are false, and (iii) all propositions are true. Such a truth assignment can be represented using only a finite amount of memory. Henceforth, we identify a state by the set of literals that are satisfied by the state. If neither of the literals for a proposition appears in the set, then the proposition is undefined in the state. Thus the empty set denotes the state in which all propositions are undefined. Unless specified otherwise, it is assumed<sup>3</sup> that  $q_0 = \emptyset$ . Under this assumption, the cardinality of a  $\Pi$ -state is finite.

To render execution monitoring tractable, every transition function must be *finitary*, meaning that:

1. only a finite number of state variables determine if the transition is defined at a given state, and
2. the resulting state can be obtained by altering only a finite number of state variables, so that the new value of each variable is a function of only a finite number of state variables in the original state.

A finitary transition function is called an *operator*.

**Design choice 2: Conjunctive preconditions, constant effects (CPCE)** An operator can be represented by two elements:

1. a *precondition expression*, which is a boolean expression in terms of a finite number of state variables, indicating if the transition is defined at a given state, and
2. for each state variable that can potentially be altered by the transition function, an *effect expression* (a boolean expression in terms of a finite number of state variables) that computes the new value for the variable.

While this arrangement is fully general, we impose further syntactic restrictions to arrive at a representation that is optimization-friendly:

1. the precondition expression must be a *conjunction of literals*, and
2. every effect expression must be a *constant truth value*.

Operators satisfying these restrictions are called *CPCE operators*. Formally, we represent a CPCE operator by a pair  $\langle pre, eff \rangle$ , where:

*pre*: a finite set of *preconditions*, each of which is a *literal* (i.e.,  $p$  or  $\neg p$ ), such that, for each proposition  $p$ , at most one of  $p$  or  $\neg p$  belongs to the set

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<sup>2</sup>Although we focus on boolean state variables here, our scheme can be readily generalized to handle variables of finite domains.

<sup>3</sup>The proposed optimization scheme can be easily adopted to the case when this assumption does not hold.

*eff*: a finite set of **effects**, each of which is a **generalized literal** (i.e.,  $p$ ,  $\neg p$ , or  $?p$ ), such that, for each proposition  $p$ , at most one of  $p$ ,  $\neg p$  or  $?p$  appears in the set

The state obtained by applying the CPCE operator  $\langle pre, eff \rangle$  to a state  $S$  (i.e., a set of literals) is:

$$\langle pre, eff \rangle(S) = \begin{cases} S \oplus eff & \text{if } pre \subseteq S \\ \text{undefined} & \text{otherwise} \end{cases}$$

where, given a set  $P$  of propositions, a set  $S$  of literals and a set  $L$  of generalized literals,

$$\begin{aligned} S \oplus L &= (S \setminus lits(vars(L))) \cup (L \cap lits(vars(L))) \\ vars(L) &= \{p \in \Pi \mid p \in L \vee \neg p \in L \vee ?p \in L\} \\ lits(P) &= P \cup \{\neg p \mid p \in P\} \end{aligned}$$

Intuitively, the operator is defined at state  $S$  if the conjunction  $pre$  is satisfied by the truth assignment  $S$ . In the resulting state, a propositional variable  $p$  is set to true if  $p \in eff$ , false if  $\neg p \in eff$ , undefined if  $?p \in eff$ , or otherwise the same value as in the original state. As a special case, the **empty operator**  $\langle \emptyset, \emptyset \rangle$  represents the total identity function  $\iota_Q$  for monitor states. Also notice that the preconditions of an operator cannot be used for detecting if a proposition is undefined in a given state, but effects could set propositions to undefined. This intentional asymmetry serves an important function to be discussed in the proof of Theorem 10.

How this policy representation facilitates optimization will be deferred to Section 4.

### 3.3 Evaluation of Expressiveness

We evaluate the expressiveness of the proposed policy representation by a number of case studies.

#### 3.3.1 Complete Mediation

Complete Mediation [31] requires every sensitive operation to be performed only after a monitoring operation has been invoked. Here we describe a formulation of the Complete Mediation policy inspired by [35], in which the policy is applied to the context of Java stack inspection [41]. Specifically, the goal is to ensure that, in Java platform library code, every sensitive operation is guarded by a call to the stack inspection logic. Such a policy prescribes an event set  $\Sigma = \{sen, mon\}$ , where the two events correspond to, respectively, the occurrence of a sensitive operation and an invocation of stack inspection logic. To enforce the policy, a monitor is constructed with state variable set  $\Pi = \{p_m\}$ , and transition functions  $\delta_{sen} = \langle \{p_m\}, \{\neg p_m\} \rangle$  and  $\delta_{mon} = \langle \emptyset, \{p_m\} \rangle$ . Intuitively, the proposition  $p_m$  records in the current state that a monitoring operation has occurred. The transition function  $\delta_{mon}$  asserts  $p_m$  without requiring any precondition. The transition function  $\delta_{sen}$  is enabled when  $mon$  has occurred. The occurrence of  $sen$  also negates  $p_m$ , thus ensuring that every subsequent occurrence of  $sen$  is preceded by a  $mon$ .

#### 3.3.2 Separation of Duty

Separation of Duty (Section 3.1, Figure 1) prescribes an access event set  $\Sigma = \{a, m, c\}$ . The policy is enforced by a monitor for which  $\Pi = \{p_a, p_m\}$ , where  $p_a$  and  $p_m$  indicate, respectively,

that events  $a$  and  $m$  have occurred. The transition functions are defined as follows:  $\delta_a = \langle \emptyset, \{p_a\} \rangle$ ,  $\delta_m = \langle \emptyset, \{p_m\} \rangle$ ,  $\delta_c = \langle \{p_a, p_m\}, \{\neg p_a, \neg p_m\} \rangle$ . The monitor ensures that  $c$  only occurs after both  $a$  and  $m$  have occurred, without imposing an ordering of  $a$  and  $m$ .

### 3.3.3 Generalized Chinese Wall Policy

The Chinese Wall Policy [9] prevents conflicts of interest that may arise from allowing access to data sets that belong to competing parties. Lin proposed a generalization, in which conflict relationships need not form an equivalence relation [26]. In extensible systems, Lin’s Generalized Chinese Wall Policy can be employed to ensure that conflicting operations are not executed by an untrusted component, thereby protecting the integrity of the application core. Formally, a Generalized Chinese Wall Policy is characterized by a conflict graph  $\langle \Sigma, E \rangle$ , where  $\Sigma$  is a countable set of operations, and each undirected edge in  $E$  connects a pair of operations in conflict with one another. Execution of an operation  $a \in \Sigma$  renders all neighbors of  $a$  forbidden in the future. Under the mild assumption that vertices of the conflict graph has bounded degrees, the Generalized Chinese Wall Policy can be expressed as CPCE operators as follows. Define  $\Pi = \{p_a \mid a \in \Sigma\}$ ,  $q_0 = \{\neg p_a \mid a \in \Sigma\}$ , and set  $\delta_a = \langle \{\neg p_b \mid ab \in E\}, \{p_a\} \rangle$ . The construction ensures that the set of executed operations is always an independent set in the conflict graph.

### 3.3.4 Hierarchical One-Out-Of- $k$ Authorization

One-out-of- $k$  authorization [13, 16] classifies applications into equivalence classes based on the access rights required for successful execution. For example, a *browser* needs the right to open network connections but never accesses user files, and an *editor* needs the right to access user files but never connects to the network. The protection goal is to ensure that untrusted code only exercises the access rights of a known application class: e.g., an application that both reads a user file and connects to the network is neither a browser nor editor, and thus must be rejected. Formally, an One-Out-Of- $k$  Policy is characterized by a family  $\{\mathcal{C}_i\}_{1 \leq i \leq k}$  of application classes such that  $\mathcal{C}_i \subseteq \Sigma$ . The policy requires that, every time a program is executed, there is a  $\mathcal{C}_i$  such that every access right exercised during that execution belongs to  $\mathcal{C}_i$ . One-out-of- $k$  authorization, in its full generality, is not necessarily expressible as CPCE operators.

**Theorem 1.** *There is an One-Out-Of- $k$  Policy that cannot be enforced by CPCE operators.*

*Proof.* Consider the One-Out-Of- $k$  Policy for which  $\Sigma = \{a_0, a_1, a_2\}$  and  $\mathcal{C}_i = \{a_i, a_{((i+1) \bmod 3)}\}$  for  $0 \leq i < 3$ . By way of contradiction, assume that there is a set  $\Pi$  of propositions, an initial state  $q_0$  and transition functions  $\delta_{a_i}$ , for  $0 \leq i < 3$ , that enforce the policy. Because  $a_0 a_1 a_2$  is not a safe sequence, there must be a literal  $l \in \delta_{a_2}.pre$  such that  $l \notin \delta_{a_0 a_1}(q_0)$ . But then  $a_0 a_2$  is safe, which means  $l \in \delta_{a_0}(q_0)$ . Consequently, it must be the case that  $\bar{l} \in \delta_{a_1}.eff$ , where  $\bar{l}$  is the negation of literal  $l$ , or else the change of membership of  $l$  between  $\delta_{a_0}(q_0)$  and  $\delta_{a_0 a_1}(q_0)$  would not have occurred. Now  $\delta_{a_1 a_2}(q_0)$  is not defined, contradicting the fact that  $a_1 a_2$  is a safe sequence.  $\square$

Fortunately, there is an important special case of one-out-of- $k$  that the CPCE representation can capture.

**Definition 2.** An One-Out-Of- $k$  Policy  $\{\mathcal{C}_i\}_{1 \leq i \leq k}$  is said to be **hierarchical** iff both of the following hold:

$$\forall i, j. \mathcal{C}_i \cap \mathcal{C}_j \neq \emptyset \Rightarrow \exists m. \mathcal{C}_m = \mathcal{C}_i \cap \mathcal{C}_j \quad (1)$$

$$\forall i, j, m. (\mathcal{C}_i \subseteq \mathcal{C}_m \wedge \mathcal{C}_j \subseteq \mathcal{C}_m) \Rightarrow (\mathcal{C}_i \subseteq \mathcal{C}_j \vee \mathcal{C}_j \subseteq \mathcal{C}_i) \quad (2)$$

Condition (1) asserts that the family of application classes is closed under non-empty intersection. Condition (2) asserts that the subclasses of any given class are totally ordered. The Hasse diagram [12] of classes satisfying the two conditions is a forest (hence “hierarchical”).

**Theorem 3.** Every hierarchical One-Out-Of- $k$  Policy is enforceable by CPCE operators.

*Proof.* Consider a Hierarchical One-Out-Of- $k$  Policy  $\{\mathcal{C}_i\}_{1 \leq i \leq k}$ . Without loss of generality, assume that every  $a \in \Sigma$  belongs to at least one  $\mathcal{C}_i$ . Define the **home class**  $\mathcal{H}(a)$  of access  $a \in \Sigma$  to be  $\bigcap \{\mathcal{C} \in \{\mathcal{C}_i\}_{1 \leq i \leq k} \mid a \in \mathcal{C}\}$ , that is, the smallest class containing  $a$ . (The existence of such a class is guaranteed by condition (1).) A pair of accesses, say  $a$  and  $b$ , is said to be **consistent** iff they belong to the same application class: i.e.,  $\exists i. \{a, b\} \subseteq \mathcal{C}_i$ . Otherwise, they are **in conflict**. Notice that  $a$  and  $b$  are consistent iff  $\mathcal{H}(a) \subseteq \mathcal{H}(b) \vee \mathcal{H}(b) \subseteq \mathcal{H}(a)$ . (The “if” direction is immediate. The “only if” direction follows from  $\{a, b\} \subseteq \mathcal{C}_i$  by an application of condition (2).)

To obtain the required CPCE representation of  $\{\mathcal{C}_i\}_{1 \leq i \leq k}$ , construct  $\Pi = \{p_{\mathcal{C}} \mid \mathcal{C} \in \{\mathcal{C}_i\}_{1 \leq i \leq k}\}$ ,  $q_0 = \{\neg p_{\mathcal{C}} \mid \mathcal{C} \in \{\mathcal{C}_i\}_{1 \leq i \leq k}\}$ , and  $\delta_a = \langle pre_a, eff_a \rangle$ , where:

$$pre_a = \{\neg p_{\mathcal{C}} \mid \mathcal{H}(a) \not\subseteq \mathcal{C} \wedge \mathcal{C} \not\subseteq \mathcal{H}(a)\}$$

$$eff_a = \{p_{\mathcal{H}(a)}\}$$

It is easy to see that, with the CPCE operators above, at run time, the set  $H$  of accesses that have occurred so far are pair-wise consistent. What we want is that there is a  $\mathcal{C}_i$  such that  $H \subseteq \mathcal{C}_i$ . We prove this by induction.

The base cases for  $|H| \leq 2$  can be handled trivially. Suppose, for some  $k > 2$ , all event set  $H$  with  $|H| = k$  is such that  $H \subseteq \mathcal{C}_i$  for some  $i$  whenever  $H$  contains pairwise-consistent events. Consider a set  $H' = H \cup \{a\}$  where  $|H| = k$ ,  $a \notin H$ , and events in  $H'$  are pairwise consistent. By way of contradiction, assume the following holds:

$$\text{There is no } \mathcal{C}_i \text{ such that } H' \subseteq \mathcal{C}_i. \quad (3)$$

Because  $H$  contains pairwise-consistent events, the induction hypothesis implies that there is a class  $\mathcal{C}^*$  such that  $H \subseteq \mathcal{C}^*$ . Also,  $a$  is consistent with every member of  $H$ . Thus, for each  $b \in H$ , let  $\mathcal{C}_b$  be a class containing both  $a$  and  $b$ . By (1),  $\mathcal{C}^\circ = \bigcap_{b \in H} \mathcal{C}_b$  is a class. By assumption (3), there is an event  $b^* \in H$  such that  $b^* \notin \mathcal{C}^\circ$ . By (1),  $\mathcal{C}^\bullet = \mathcal{C}^* \cap \mathcal{C}_{b^*}$  is a class. Now,  $a \in \mathcal{C}^\circ$ , but  $a \notin \mathcal{C}^\bullet$ ;  $b^* \in \mathcal{C}^\bullet$ , but  $b^* \notin \mathcal{C}^\circ$ . So  $\mathcal{C}^\circ$  and  $\mathcal{C}^\bullet$  are distinct, incomparable subsets of  $\mathcal{C}_{b^*}$ , contradicting (2).  $\square$

Although the construction of Theorem 3 is representationally sufficient, that encoding of Hierarchical One-Out-Of- $k$  Policies by CPCE operators could lead to precondition and effect sets having a size of  $O(k)$ . When  $k$  is large, such an encoding incurs a significant performance overhead (see Section 4 for a precise definition of performance overhead). The following theorem demonstrates that there is occasionally a more efficient encoding. For hierarchies with a few balanced trees, in which the height of the hierarchy is logarithmically related to the number of application classes and the branching factor is bounded by a constant, the following policy encoding leads to precondition or effect sets of size  $O(\log k)$ .

**Theorem 4.** *There is a CPCE representation of a Hierarchical One-Out-Of- $k$  Policy  $\{\mathcal{C}_i\}_{1 \leq i \leq k}$  such that the size of each precondition or effect set is  $O(h \cdot b + r)$ , where  $h$  is the maximum tree height of the forest induced by the policy,  $b$  is the maximum branching factor, and  $r$  is the number of trees in the forest.*

*Proof.* Given a family  $\mathcal{F}$  of sets, define  $\text{minimal}(\mathcal{F}) = \{S \in \mathcal{F} \mid \forall S' \in \mathcal{F}. S' \not\subseteq S\}$ . Consider the following CPCE encoding. Define  $\Pi = \{p_{\mathcal{C}} \mid \mathcal{C} \in \{\mathcal{C}_i\}_{1 \leq i \leq k}\}$ ,  $q_0 = \{\neg p_{\mathcal{C}} \mid \mathcal{C} \in \{\mathcal{C}_i\}_{1 \leq i \leq k}\}$  and set  $\delta_a = \langle \text{pre}_a, \text{eff}_a \rangle$ , where

$$\begin{aligned} \text{pre}_a &= \{\neg p_{\mathcal{C}} \mid \mathcal{C} \in \text{minimal}(\{\mathcal{C}_i \mid \mathcal{C}_i \not\subseteq \mathcal{H}(a) \vee \mathcal{H}(a) \not\subseteq \mathcal{C}_i\})\} \\ \text{eff}_a &= \{p_{\mathcal{C}_i} \mid \mathcal{C}_i \subseteq \mathcal{H}(a)\} \end{aligned}$$

We claim that this operator formulation is equivalent to the one defined in the proof of Theorem 3. To establish the claim, it suffices to show that, for every  $a, b \in \Sigma$ ,  $\mathcal{H}(a) \subseteq \mathcal{H}(b) \vee \mathcal{H}(b) \subseteq \mathcal{H}(a)$  iff  $\mathcal{H}(a) \subseteq \mathcal{C}_i \vee \mathcal{C}_i \subseteq \mathcal{H}(a)$  for every  $\mathcal{C}_i \subseteq \mathcal{H}(b)$ . The “if” direction is immediate. Consider the “only if” direction. In the case when  $\mathcal{H}(b) \subseteq \mathcal{H}(a)$ , the claimed consequent is immediate. In the case when  $\mathcal{H}(a) \subseteq \mathcal{H}(b)$ , the claimed consequent follows from condition (2).

$|\text{eff}_a|$  is obviously  $O(h)$ . To obtain a bound on  $|\text{pre}_a|$ , notice that  $\text{pre}_a$  contains those literals  $\neg p_{\mathcal{C}}$  for two types of class  $\mathcal{C}$ . Firstly,  $\mathcal{C}$  may be the root of a tree completely disjoint from the tree in which  $\mathcal{H}(a)$  belongs. There are at most  $O(r)$  of these literals. Secondly,  $\mathcal{C}$  may be a child of an ancestor of  $\mathcal{H}(a)$ . There are at most  $h \times (b - 1) = O(h \cdot b)$  of these literals. The bound in the statement of this theorem follows immediately.  $\square$

Most naturally-occurring One-Out-Of- $k$  Policies are either hierarchical, or can be made hierarchical without affecting safety (e.g., the policy in [16, Section 4.3] is an example). To demonstrate this, we begin with the following definition:

**Definition 5.** *The **intersection closure** of an One-Out-Of- $k$  Policy  $\{\mathcal{C}_i\}_{1 \leq i \leq k}$  is the following family of application classes:*

$$\text{clos}(\{\mathcal{C}_i\}_{1 \leq i \leq k}) = \left\{ \bigcap_{i \in H} \mathcal{C}_i \mid H \subseteq \{1, 2, \dots, k\} \wedge H \neq \emptyset \right\} \setminus \{\emptyset\}$$

*An One-Out-Of- $k$  Policy  $\{\mathcal{C}_i\}_{1 \leq i \leq k}$  is said to be **proto-hierarchical** iff  $\text{clos}(\{\mathcal{C}_i\}_{1 \leq i \leq k})$  is hierarchical.*

**Theorem 6.** *Given a proto-hierarchical policy  $\{\mathcal{C}_i\}_{1 \leq i \leq k}$ , an equivalent hierarchical policy  $\{\mathcal{C}'_j\}_{1 \leq j \leq k'}$  can be constructed, such that  $k' = O(k)$ .*

*Proof.* Construct  $\{\mathcal{C}'_j\}_{1 \leq j \leq k'} = \text{clos}(\{\mathcal{C}_i\}_{1 \leq i \leq k})$ . By definition,  $\{\mathcal{C}'_j\}_{1 \leq j \leq k'}$  is hierarchical.

We show that  $\{\mathcal{C}'_j\}_{1 \leq j \leq k'}$  is equivalent to  $\{\mathcal{C}_i\}_{1 \leq i \leq k}$ . Suppose an event sequence  $w$  is permitted by  $\{\mathcal{C}_i\}_{1 \leq i \leq k}$ . Then there is some  $\mathcal{C}_i$  such that every event occurring in  $w$  is a member of  $\mathcal{C}_i$ . By construction  $\mathcal{C}_i \in \{\mathcal{C}'_j\}_{1 \leq j \leq k'}$ , hence  $w$  is permitted by  $\{\mathcal{C}'_j\}_{1 \leq j \leq k'}$ . Conversely, suppose an event sequence  $w$  is permitted by  $\{\mathcal{C}'_j\}_{1 \leq j \leq k'}$ . Then there is some  $\mathcal{C}'_j$  such that every event occurring in  $w$  is a member of  $\mathcal{C}'_j$ . By construction, there is a  $\mathcal{C}_i$  such that  $\mathcal{C}'_j \subseteq \mathcal{C}_i$ , hence  $w$  is permitted by  $\{\mathcal{C}_i\}_{1 \leq i \leq k}$ .

We show that  $k' = O(k)$ . A class  $\mathcal{C}'_j$  is said to be *synthetic* iff  $\mathcal{C}'_j \notin \{\mathcal{C}_i\}_{1 \leq i \leq k}$ . As pointed out previously, the Hasse diagram of  $\{\mathcal{C}'_j\}_{1 \leq j \leq k'}$  is a forest. Observe that, by construction, every synthetic class has more than one child. By simple induction, it can be shown that the number of synthetic classes is strictly less than  $k$  (i.e., the number of non-synthetic classes). The required bound follows.  $\square$

Theorems 4 and 6 together imply that there is an efficient CPCE encoding of proto-hierarchical policies.

**Example 7.** Consider the One-Out-Of-3 Policy,  $\{\mathcal{C}_i\}_{1 \leq i \leq 3}$ , taken from [16, Section 4.3], for which the event set  $\Sigma$  is the following:

$$\{ \text{access-tmp-files, access-usr-files, connect-to-network, console-io, create-subprocess} \}$$

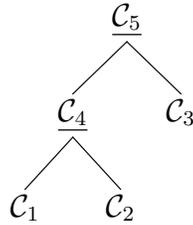
and the application classes are:

$$\begin{aligned} \text{browser :} & \quad \mathcal{C}_1 = \{ \text{connect-to-network, access-tmp-files, console-io} \} \\ \text{editor :} & \quad \mathcal{C}_2 = \{ \text{access-usr-files, access-tmp-files, console-io} \} \\ \text{shell :} & \quad \mathcal{C}_3 = \{ \text{console-io, create-subprocess} \} \end{aligned}$$

According to Definition 2, the policy is not hierarchical, for the set  $\mathcal{C}_1 \cap \mathcal{C}_2 = \{ \text{access-tmp-files, console-io} \}$  is not an application class, thus violating condition (1). It is easy to verify that the policy is proto-hierarchical (Definition 5), for its intersection closure  $\{\mathcal{C}_i\}_{1 \leq i \leq 5}$  is hierarchical, where the synthetic classes (Theorem 6) are listed below:

$$\begin{aligned} \mathcal{C}_4 &= \{ \text{access-tmp-files, console-io} \} \\ \mathcal{C}_5 &= \{ \text{console-io} \} \end{aligned}$$

The (inverted) Hasse diagram of this hierarchy is shown below, with the synthetic classes underlined:



The construction in the proof of Theorem 3 gives us a CPCE encoding of  $\{\mathcal{C}_i\}_{1 \leq i \leq 5}$ . The following table lists the home class, effect set and precondition set of every event:

$a$	$\mathcal{H}(a)$	$eff_a$	$pre_a$
access-tmp-files	$\mathcal{C}_4$	$\{pc_4\}$	$\{\neg pc_3\}$
access-usr-files	$\mathcal{C}_2$	$\{pc_2\}$	$\{\neg pc_1, \neg pc_3\}$
connect-to-network	$\mathcal{C}_1$	$\{pc_1\}$	$\{\neg pc_2, \neg pc_3\}$
console-io	$\mathcal{C}_5$	$\{pc_5\}$	$\{\}$
create-subprocess	$\mathcal{C}_3$	$\{pc_3\}$	$\{\neg pc_1, \neg pc_2, \neg pc_4\}$

The alternative CPCE encoding described in the proof of Theorem 4 yields a different set of operators:

$a$	$\mathcal{H}(a)$	$eff_a$	$pre_a$
<i>access-tmp-files</i>	$\mathcal{C}_4$	$\{pc_4, pc_5\}$	$\{\neg pc_3\}$
<i>access-usr-files</i>	$\mathcal{C}_2$	$\{pc_2, pc_4, pc_5\}$	$\{\neg pc_1, \neg pc_3\}$
<i>connect-to-network</i>	$\mathcal{C}_1$	$\{pc_1, pc_4, pc_5\}$	$\{\neg pc_2, \neg pc_3\}$
<i>console-io</i>	$\mathcal{C}_5$	$\{pc_5\}$	$\{\}$
<i>create-subprocess</i>	$\mathcal{C}_3$	$\{pc_3, pc_5\}$	$\{\neg pc_4\}$

The difference between the two encoding is the most visible in the case of *create-subprocess*. The first encoding yields a singleton effect set, and a precondition set that could have a size comparable to that of the hierarchy itself (imagine there are subtrees below  $\mathcal{C}_1$  and  $\mathcal{C}_2$ ). The second encoding yields an effect set with a size proportional to the height of the tree, and a precondition set with a size proportional to the branching factor of the tree.

## 4 The Basic Optimization Procedure

Given a program represented as control flow graphs (CFGs) [19, 6], an IRM enforcement mechanism proceeds in three phases:

**Phase 1:** By consulting a security policy, construct an associative array  $op[\cdot]$ , assigning to every program point  $n$  some (possibly empty) operator  $op[n]$ .

**Phase 2:** Optimize the operator assignment by updating the entries in  $op[\cdot]$ , in some semantic-preserving manner, with the objective that the resulting execution time is improved.

**Phase 3:** Instrument the target program by injecting, (a) at the program entry point, a code fragment that initializes a globally accessible monitor state, and, (b) at each program point  $n$ , a code fragment simulating  $op[n]$ . The latter code fragment will behave as follows at run time:

- The preconditions in  $op[n].pre$  are checked against the current monitor state. If any of the preconditions is not satisfied, then a security exception is raised<sup>4</sup>.
- The effects are asserted into the monitor state.

The focus of this work is **Phase 2** — the design of optimization procedures.

Given  $op[\cdot]$ , a control flow path is *feasible* iff all operator preconditions are satisfied along the path. Unlike [11], which assumes all transitions to have the same cost, we adopt the following performance metric: the *overhead* of a feasible path is the total number of preconditions checked and effects asserted along the path. More precisely, an operator  $\langle pre, eff \rangle$  incurs an overhead of  $|pre| + |eff|$  every time it is executed. The fewer preconditions and effects are involved in an operator, the less overhead it incurs on the target program. For example, the empty operator does not impose an overhead of zero. This performance metric is adopted because the number of propositions appearing in a  $\Pi$ -state can in principle be unbounded, and thus no constant-time implementation of transitions is available.

An *execution trace* is a control flow path that starts at the entry point of the program. An optimization procedure is *sound* iff infeasible execution traces remain infeasible, and *transparent* iff

<sup>4</sup>It is assumed that the target program cannot catch such an exception. How this can be enforced will be further discussed in Section 7.

feasible execution traces remain feasible<sup>5</sup>. Ensuring soundness is central to the security enterprise. A sound optimization procedure is *effective* iff, (a) the overhead of a feasible execution trace is never increased by the procedure, and (b) there is at least one program and a feasible execution trace for that program such that the overhead is strictly reduced by the procedure. Notice that the notion of effectiveness is only defined for sound optimization.

We focus on two kinds of optimization: precondition and effect elimination. That is, the optimization procedure eliminates redundant members of  $op[n].pre$  and  $op[n].eff$ . As the overhead of a feasible path is never increased by precondition and effect elimination, such an optimization procedure is always effective so long as it is sound. The remaining challenge is to conduct precondition and effect elimination without sacrificing soundness or transparency.

## 4.1 Simple Programs

### 4.1.1 Program Representation

We describe how precondition and effect elimination can be performed for simple programs, each of which is represented as a control flow graph. Initiating the discussion with such a simple representation allows us to introduce key concepts in an easily comprehensible form. Specifically, a control flow graph is a tuple  $\langle N, n_{entry}, n_{exit}, N_{instr}, E \rangle$ :

- $N$  is a set of nodes, partitioned into  $\{n_{entry}\} \cup \{n_{exit}\} \cup N_{instr}$ . The distinguished nodes  $n_{entry}$  and  $n_{exit}$  are the entry and exit nodes of the program.  $N_{instr}$  is the set of instruction nodes, which correspond to actual program instructions.
- $E$  is a set of directed edges, such that  $E \subseteq (\{n_{entry}\} \cup N_{instr}) \times (\{n_{exit}\} \cup N_{instr})$ . Intuitively, the subset requirement mandates that  $n_{entry}$  is a source, and  $n_{exit}$  is a sink.

The sets of predecessors and successors of  $n$  in a set  $E'$  of edges are defined as follows:

$$\begin{aligned} pred[n | E'] &= \{ m \in N \mid (m, n) \in E' \} \\ succ[n | E'] &= \{ m \in N \mid (n, m) \in E' \} \end{aligned}$$

We also write  $pred[n]$  and  $succ[n]$  for  $pred[n | E]$  and  $succ[n | E]$  respectively.

An *execution trace* is simply a control flow path starting at  $n_{entry}$ .

### 4.1.2 Optimization Procedure

The input to the optimization procedure consists of the following:

- a program  $\langle N, n_{entry}, n_{exit}, N_{instr}, E \rangle$
- an operator assignment  $op[\cdot]$  that maps each node<sup>6</sup> to an operator (henceforth, we assume that  $op[n] = \langle \emptyset, \emptyset \rangle$  initially for  $n \notin N_{instr}$ )

The optimization procedure proceeds in four steps, a pattern to be preserved in the sequel as we consider other program representations:

<sup>5</sup>The notions of soundness and transparency were originally defined in the work of Ligatti *et al.* [5, 23, 24, 25]. They are adapted in this work to articulate the quality of IRM optimization.

<sup>6</sup>Although we associate operators to flow graph nodes, there is no reason operators cannot be assigned to flow graph edges, as in the case of [11].

**Step 1** *Compute a conservative approximation of the guaranteed set for each program point.* A literal  $l$  belongs to the **guaranteed set** of a program point  $n$  iff  $l$  is established by every feasible path from  $n_{entry}$  to  $n$ . This forward analysis is a form of constant propagation [28]:

$$\text{GUA}_{out}[n] = (\text{GUA}_{in}[n] \oplus op[n].pre) \oplus op[n].eff \quad \text{for } n \in N_{instr} \quad (4)$$

$$\text{GUA}_{out}[n] = \emptyset \quad \text{for } n \in \{n_{entry}\} \quad (5)$$

$$\text{GUA}_{in}[n] = \bigcap_{m \in pred[n]} \text{GUA}_{out}[m] \quad \text{for } n \in N_{instr} \cup \{n_{exit}\} \quad (6)$$

Note the form of (4). By checking the preconditions, an operator has essentially ruled out infeasible paths. Those paths that remain must have the preconditions established as a result. Consequently, preconditions could be seen as **implicit assertions**, while effects are **explicit assertions**. Notice also that the order of assertion is significant: explicit assertions override implicit assertions.

**Step 2** *Eliminate the redundant preconditions.* A precondition  $l$  is considered redundant at program point  $n$  if  $l$  is guaranteed to be established at  $n$ .

$$op[n].pre := op[n].pre \setminus \text{GUA}_{in}[n] \quad \text{for } n \in N_{instr} \quad (7)$$

When a precondition is removed, the implicit assertion associated with the precondition is also removed. This does not affect soundness, as both the precondition check and the associated implicit assertion are already guaranteed to be established.

**Step 3** *Compute a conservative approximation of the live set at each program point.* A proposition  $p$  is **live** at program point  $n$  iff there is a path from  $n$  to another program point  $n'$  such that (1)  $p$  is checked at  $n'$ , and (2) there is no (implicit or explicit) effect assertion involving  $p$  along any path from  $n$  to  $n'$  [28]. This backward analysis is defined as follows:

$$\text{LIV}_{in}[n] = (\text{LIV}_{out}[n] \setminus kill_{\text{LIV}}[n]) \cup gen_{\text{LIV}}[n] \quad \text{for } n \in N_{instr} \quad (8)$$

$$\text{LIV}_{in}[n] = \emptyset \quad \text{for } n \in \{n_{exit}\} \quad (9)$$

$$\text{LIV}_{out}[n] = \bigcup_{m \in succ[n]} \text{LIV}_{in}[m] \quad \text{for } n \in N_{instr} \cup \{n_{entry}\} \quad (10)$$

where, for  $n \in N_{instr}$ ,

$$kill_{\text{LIV}}[n] = vars(op[n].eff)$$

$$gen_{\text{LIV}}[n] = vars(op[n].pre)$$

Note that the preconditions eliminated in **Step 2** are not considered in this step. That is, effect elimination is performed on the updated version of  $op[n]$ . Also,  $kill_{\text{LIV}}[n]$  could have been defined as  $vars(op[n].pre) \cup vars(op[n].eff)$  to explicitly account for implicit assertions. We opt for a less redundant formulation because propositions in  $vars(op[n])$  are generated by  $gen_{\text{LIV}}[n]$  anyway.

**Step 4** *Eliminate the redundant effects.* A proposition is **dead** at program point  $n$  iff it is not live at  $n$ . An effect is considered redundant if the effect proposition is dead at the program point where the effect is asserted.

$$op[n].eff := op[n].eff \cap \{p, \neg p, ?p \mid p \in \text{LIV}_{out}[n]\} \quad \text{for } n \in N_{instr} \quad (11)$$

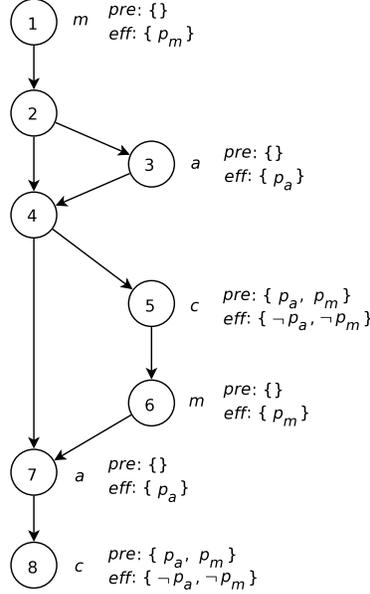


Figure 2: Control flow graph of example program in Figure 1, with operators in Section 3.3.2.

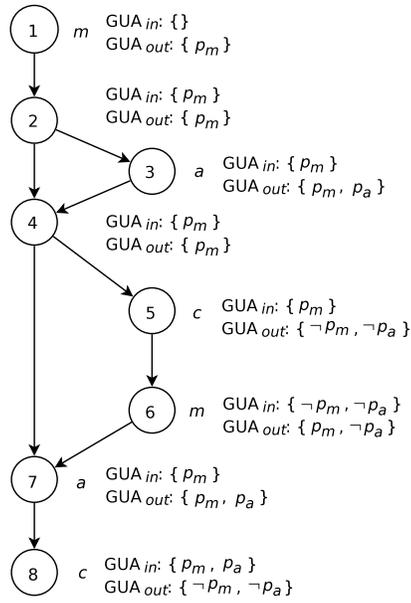
**Example 8.** Consider again the running example in Figure 1. The control flow graph of the program in Figure 1 (a) is depicted in Figure 2 along with the operators specified in Section 3.3.2. After applying **Step 1** of the optimization procedure, we obtain the guaranteed sets shown in Figure 3 (a). **Step 2** then eliminates the preconditions that are already guaranteed, resulting in the revised operators shown in 3 (b). For instance, at node 5, since  $GUA_m[5] = \{p_m\}$ , the precondition set is updated to  $\{p_a, p_m\} \setminus \{p_m\} = \{p_a\}$ . Taking the updated operators in Figure 3 (b) as input, the result of liveness analysis (**Step 3**) is given in Figure 3 (c). According to this analysis, none of the effect assertions related to the proposition  $p_m$  needs to be retained, and effect assertions related to the proposition  $p_a$  can be eliminated except for nodes 1–4. Figure 3 (d) shows the final result after the four-step optimization procedure.

**Theorem 9.** The four-step optimization procedure is sound, transparent and effective.

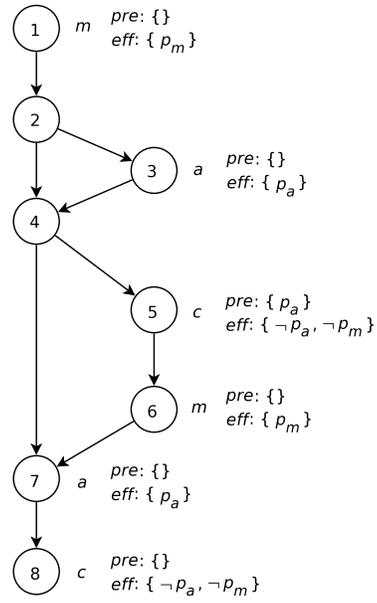
*Proof.* Since only guaranteed preconditions and dead effects are eliminated, the feasibility of a path is not altered by the optimization procedure. Soundness and transparency thus follow. Effectiveness follows from the fact that the procedure performs only precondition and effect elimination.  $\square$

**Discussion** Precondition elimination (**Step 2**) achieves more than removing unnecessary checks; by reducing the number of live propositions, **Step 2** also creates optimization opportunities for effect elimination (**Step 4**). However, **Step 2** and **Step 4** are both “optional”. Neither is dependent on the other. The optimization procedure remains sound and transparent even if one of the two steps is omitted.

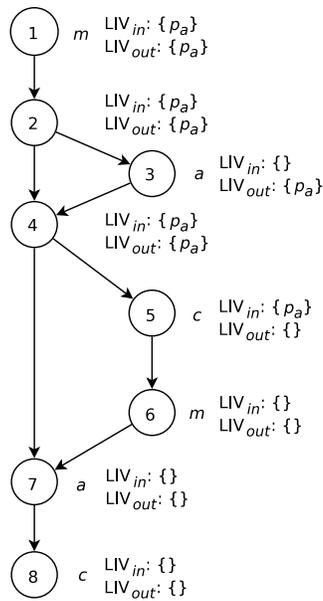
By adopting conjunctive preconditions and constant effects, rather than unconstrained precondition and effect expressions, we have obtained an elegant and informed optimization procedure. First, a function of the form  $f_L(S) = S \oplus L$  for a fixed set  $L$  of generalized literals is a monotone



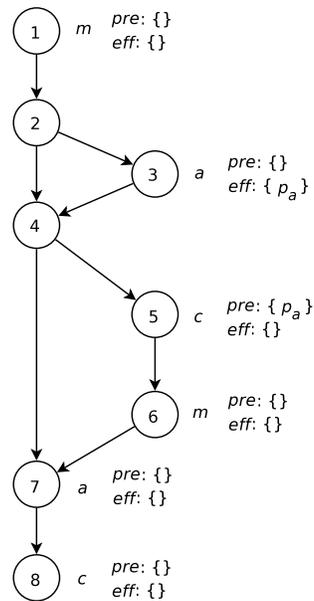
(a) After Step 1



(b) After Step 2



(c) After Step 3



(d) After Step 4

Figure 3: Four-step optimization

function [28]. Our representation is thus readily amenable to guaranteed set analysis. Second, the syntactic restriction allows the analyses to deduce more information about guaranteed sets and live sets than an unconstrained representation. Specifically, conjunctive preconditions are used by the guaranteed set analysis as implicit assertions, whereas constant effects can be exploited fully as explicit assertions (see (4)). Allowing arbitrary boolean formulas as preconditions and effects will yield much less definite information for guaranteed set analysis. A similar argument can be made for liveness analysis (see (8)) as well.

## 4.2 Procedure Calls

### 4.2.1 Program Representation

To accommodate programs made up of multiple procedures, we extend our program representation, so that a program is a collection of CFGs, one for each procedure. Specifically, a program is a tuple  $\langle ID, id_{main}, CFG, proc, invoke \rangle$ , such that:

- $ID$  is a set of procedure identifiers.
- $id_{main} \in ID$  is a distinguished procedure identifier, called the main procedure, that represents the global entry point of the program.
- $CFG$  is a set of control flow graphs with disjoint node and edge sets. Each control flow graph is a tuple  $\langle N, n_{entry}, n_{exit}, N_{call}, N_{ret}, N_{instr}, E \rangle$ , such that:
  - $N$  is a set of nodes. The set is partitioned into five disjoint subsets:  $\{n_{entry}\}$ ,  $\{n_{exit}\}$ ,  $N_{call}$ ,  $N_{ret}$  and  $N_{instr}$ . Besides the previously introduced node types,  $N_{call}$  is the set of **call nodes**, and  $N_{ret}$  is the set of **return nodes**.  $N_{call}$  and  $N_{ret}$  must have the same size.
  - A well-formed control flow graph must have an edge set  $E$  that can be partitioned into two disjoint subsets:  $E_{reg}$  and  $E_{inv}$ . They are respectively the **regular edges** and **invocation edges**. They must honor the following constraints:

$$\begin{aligned} E_{reg} &\subseteq (N_{instr} \cup N_{ret} \cup \{n_{entry}\}) \times (N_{instr} \cup N_{call} \cup \{n_{exit}\}) \\ E_{inv} &\subseteq N_{call} \times N_{ret} \end{aligned}$$

Each invocation edge represents a procedure invocation. In addition,  $E_{inv}$  must define a bijection from  $N_{call}$  to  $N_{ret}$ . This requirement is reflected in our notation: if  $(n, n') \in E_{inv}$ , then we write  $E_{inv}(n)$  and  $E_{inv}^{-1}(n')$  to denote  $n'$  and  $n$  respectively.

Fixing  $CFG$ , we write  $N^*$  to represent the union of all node sets. Notations such as  $N_{call}^*$ ,  $N_{exit}^*$ ,  $E^*$  and  $E_{inv}^*$  can be defined similarly.

- $proc : ID \rightarrow CFG$  is a bijection mapping procedure identifiers to control flow graphs.
- $invoke : N_{call}^* \rightarrow ID$  is a function mapping call nodes to procedure identifiers.

One of the reasons for carefully articulating the program representation is to ensure that control flow paths and execution traces are properly defined, so that key notions such as soundness, transparency and effectiveness are properly defined as well. Specifically, an execution trace can be defined in a mutually recursive manner, as in Figure 4.

- 
- A *G-local entry path*, where  $G$  is a control flow graph (i.e., a procedure body), is a path beginning with the entry node of  $G$ , ending at any node in  $G$ , and traversing only the edges of  $G$  (possibly including edges that are not regular).
  - A *G-local ground entry path*, where  $G$  is a control flow graph, is a  $G$ -local entry path that traverses *only* regular edges.
  - A *G-local expanded entry path*, where  $G$  is a control flow graph, is one of the following:
    - [LEEP-1] a  $G$ -local ground entry path
    - [LEEP-2] a sequence of nodes that can be constructed as follows: take a  $G$ -local entry path, and, for each invocation edge traversed, insert between the corresponding call node and return node a  $G'$ -local expanded entry path that ends at the exit node of  $G'$ , where  $G'$  is the procedure invoked by the invocation edge
    - [LEEP-3] a path that can be constructed by concatenating the following two sequences:
      - (i) a  $G$ -local expanded entry path ending with a call node for procedure  $G'$ , and (ii) a  $G'$ -local expanded entry path
  - An *execution trace* is a  $G$ -local expanded entry path, where  $G$  is the body of the main procedure.
- 

Figure 4: Definition of execution traces for programs with procedure calls.

## 4.2.2 Optimization Procedure

We envision a modular optimization scheme, in which the four-step optimization procedure is applied to CFGs one at a time, and the order in which CFGs are processed is not material. This allows the optimization procedure to be performed at program loading time in an environment supporting lazy, dynamic linking. (The Java Virtual Machine (JVM) is such an environment.) To this end, we adjust data flow equations (5), (6), (9) and (10) as follows:

$$\text{GUA}_{out}[n] = \emptyset \quad \text{for } n \in N_{ret} \cup \{n_{entry}\} \quad (12)$$

$$\text{GUA}_{in}[n] = \bigcap_{m \in \text{pred}[n]} \text{GUA}_{out}[m] \quad \text{for } n \in N_{instr} \cup N_{call} \cup \{n_{exit}\} \quad (13)$$

$$\text{LIV}_{in}[n] = \Pi \quad \text{for } n \in N_{call} \cup \{n_{exit}\} \quad (14)$$

$$\text{LIV}_{out}[n] = \bigcup_{m \in \text{succ}[n]} \text{LIV}_{in}[m] \quad \text{for } n \in N_{instr} \cup N_{ret} \cup \{n_{entry}\} \quad (15)$$

While (13) and (15) are cosmetic changes, (12) and (14) pose significant challenges:

**Challenge #1** On entry to a procedure, no knowledge about the caller’s state at the call node is available. We are forced to assume the guaranteed set at the procedure entry node is empty (i.e., (12)), thereby reducing the opportunities for precondition elimination within the procedure body.

**Challenge #2** On exit from a procedure, no knowledge about the caller’s live set at the return node is available. We are forced to assume that all propositions are live (i.e., (14)), thereby reducing the opportunities for effect elimination within the procedure body.

**Challenge #3** By (14), effects asserted prior to a call node cannot be readily eliminated.

**Challenge #4** By (12), precondition checks following a return node cannot be readily eliminated.

In the next section, we discuss a distributed optimization protocol that would allow an untrusted code producer to assist a distrusting code consumer in addressing the above challenges.

## 5 A Distributed Optimization Protocol

### 5.1 Cooperative Optimization without Assuming Trust

Consider a program distribution scenario inspired by [27], in which an untrusted code producer  $\mathcal{P}$  distributes a program  $\mathbb{P}$  to a code consumer  $\mathcal{C}$  for execution. Suppose  $\mathcal{C}$  employs IRM to enforce a history-based access control policy, while  $\mathcal{P}$ , eager to promote the usage of  $\mathbb{P}$ , offers to help boost the optimization effectiveness of  $\mathcal{C}$ . How can  $\mathcal{C}$  securely accept the contribution of  $\mathcal{P}$ ? We propose the following *distributed optimization protocol*.

**Stage 1:**  $\mathcal{C}$  publishes, over an *untrusted* media, a security policy  $\pi = \langle \Pi, \{\delta_a\}, \alpha \rangle$ , where  $\Pi$  is a set of state variables,  $\{\delta_a\}$  a family of operators for  $\Pi$ -states, and  $\alpha$  a procedure that computes, for a program  $\mathbb{P}$ , an associative array  $op[\cdot]$  mapping every program point in  $\mathbb{P}$  to an operator from  $\{\delta_a\}$ .

**Stage 2:**  $\mathcal{P}$  submits  $\pi$  and an *untrusted* program  $\mathbb{P}$  to an *untrusted oracle*, which generates a set  $D$  of *optimization directives*.  $D$  contains annotations designed to inform  $\mathcal{C}$  of how aggressive optimization can be achieved.

**Stage 3:**  $\mathcal{P}$  ships the package  $\langle \mathbb{P}, D \rangle$  to  $\mathcal{C}$  via an *untrusted* channel.

**Stage 4:**  $\mathcal{C}$  performs the steps below before executing  $\mathbb{P}$ :

**Phase 1:** Use procedure  $\alpha$  to construct operator assignment  $op[\cdot]$  for  $\mathbb{P}$ .

**Phase 2:** Update  $op[\cdot]$  as follows: **(a)**  $D$  is exploited to optimize  $op[\cdot]$  aggressively. **(b)** As  $D$  cannot be fully trusted, blindly following the optimization directives may destroy the soundness of the optimization procedure. Additional “guards” are injected into  $op[\cdot]$ , so that fraudulent annotations are detected when  $\mathbb{P}$  is executed.

**Phase 3:** Inject  $op[\cdot]$  into  $\mathbb{P}$ .

The protocol is particularly appropriate for a  $\mathcal{C}$  that is computationally constrained (e.g., IRM via load-time binary rewriting), and a  $\mathcal{P}$  having access to a computationally powerful oracle (e.g., offline certification service). In the sequel, we specialize the protocol for addressing the four optimization challenges outlined in Section 4.2.

## 5.2 Procedure Interfaces

We postulate that the code producer attaches a *procedure interface* to every procedure it ships. Specifically, a program is a tuple  $\langle ID, id_{main}, CFG, proc, invoke, interface \rangle$ , such that:

- $interface : ID \rightarrow (2^{bits(\Pi)} \times 2^{bits(\Pi)} \times 2^\Pi \times 2^\Pi)$  is a mapping from procedure identifiers to procedure interfaces. Each procedure interface is a tuple  $\langle pre, post, dead_{in}, dead_{out} \rangle$ , where:

*pre*: a set of literals guaranteed by the caller to be established at the call node

*post*: a set of literals guaranteed by the procedure to be established at the exit node

*dead<sub>in</sub>*: a set of propositions guaranteed by the procedure to be dead at the entry node

*dead<sub>out</sub>*: a set of propositions guaranteed by the caller to be dead at the return node

The main procedure must have an interface of  $\langle \emptyset, \emptyset, \Pi, \Pi \rangle$ . Interfaces of other procedures can be generated by the code producer using an appropriate whole-program analysis (see Appendix C for a complete algorithm).

## 5.3 Using Procedure Interfaces as Optimization Directives

The code consumer treats the procedure interfaces as optimization directives. Specifically,  $\mathcal{C}$  uses the interfaces to perform more accurate analyses in **Step 1** and **Step 3** of the four-step optimization procedure. To facilitate discussion, we write  $syntbl(n)$  as a shorthand for  $interface[invoke[n]]$  for  $n \in N_{call}^*$ .

**Step 1 - guaranteed set analysis** We replace data flow equation (12) by the following:

$$\text{GUA}_{out}[n] = pre \quad \text{for } n \in \{n_{entry}\} \quad (16)$$

$$\text{GUA}_{out}[n] = \text{symtbl}(E_{inv}^{-1}(n)).post \quad \text{for } n \in N_{ret} \quad (17)$$

(The expression  $\text{symtbl}(E_{inv}^{-1}(n))$  refers to the callee's procedure interface for  $n \in N_{ret}$ .) Rather than indiscriminately taking guaranteed sets to be  $\emptyset$  at the entry node and the return nodes, the interface components  $pre$  and  $post$  now inform guaranteed set analysis, thereby creating more opportunities for precondition elimination, and thus addressing **Challenges 1 & 4**. This works so long as  $pre$  and  $post$  are trustworthy annotations.

**Step 3 - liveness analysis** We replace data flow equation (14) by the following:

$$\text{LIV}_{in}[n] = (\Pi \setminus dead_{out}) \cup \text{vars}(op[n].pre) \quad \text{for } n \in \{n_{exit}\} \quad (18)$$

$$\text{LIV}_{in}[n] = (\Pi \setminus \text{symtbl}(n).dead_{in}) \cup \text{vars}(op[n].pre) \quad \text{for } n \in N_{call} \quad (19)$$

(The subexpression  $\text{vars}(op[n].pre)$  does not concern us for now, because, by setting  $op[n]$  initially to  $\langle \emptyset, \emptyset \rangle$  for  $n \notin N_{instr}$ , the subexpression is essentially  $\emptyset$ . It becomes indispensable when  $op[n]$  is not empty, as is the case once (20), (21) and (22) have been introduced.) If the interface components  $dead_{in}$  and  $dead_{out}$  are trustworthy, then they inform liveness analysis at the exit node and the call nodes, thereby addressing **Challenges 2 & 3**.

## 5.4 Guarding Against Fraudulent Procedure Interfaces

But the procedure interfaces are not to be trusted! They could cause essential monitoring logic to be optimized away. To prevent this, **Steps 2** and **4** of the four-step optimization procedure are adapted as follows.

**Step 2 - precondition elimination** This step now involves two subtasks. First, associate an *auxiliary operator* to the exit node and each call node:

$$op[n] := op_{guard}(\text{symtbl}(n).pre) \quad \text{for } n \in N_{call} \quad (20)$$

$$op[n] := op_{guard}(post) \quad \text{for } n \in \{n_{exit}\} \quad (21)$$

where, given a set  $S$  of literals,  $op_{guard}(S)$  is the effect-less operator  $\langle S, \emptyset \rangle$ . The injected operators guarantee that the assumptions made in data flow equations (16) and (17) are verified at run time.

The second subtask is precondition elimination, which is performed also on the newly introduced operators:

$$op[n].pre := op[n].pre \setminus \text{GUA}_{in}[n] \quad \text{for } n \in N_{instr} \cup N_{call} \cup \{n_{exit}\} \quad (22)$$

**Step 4 - effect elimination** Again, this step is now divided into two subtasks. First, an auxiliary operator is assigned to every entry and return node.

$$op[n] := op_{assert}(\text{GUA}_{out}[n], dead_{in}) \quad \text{for } n \in \{n_{entry}\} \quad (23)$$

$$op[n] := op_{assert}(\text{GUA}_{out}[n], \text{symtbl}(E_{inv}^{-1}(n)).dead_{out}) \quad \text{for } n \in N_{ret} \quad (24)$$

where, given a set  $S$  of literals and a set  $P$  of propositions,  $op_{assert}(S, P)$  is the precondition-less operator  $\langle \emptyset, (S \cap lits(P)) \cup \{?p \mid p \in P \setminus vars(S)\} \rangle$ . The operator assigns a value to each of the propositions in  $P$ . For each proposition in  $P$  that also appear in a literal in  $S$ , the assigned value is specified by the literal. For each proposition in  $P$  that does not appear in a literal in  $S$ , the assigned value is undefined. Essentially, the operator forces all propositions in  $P$  to become dead at run time, and serves as a “guard” for the assumptions made in (18) and (19).

The second subtask is effect elimination, which is also performed on the newly introduced auxiliary operators.

$$op[n].eff := op[n].eff \cap \{p, \neg p, ?p \mid p \in LIV_{out}[n]\} \quad \text{for } n \in N_{instr} \cup N_{ret} \cup \{n_{entry}\} \quad (25)$$

**Theorem 10.** *The revised optimization procedure is sound.*

*Proof.* Suppose the value of  $op[n]$  has been updated from  $\langle \emptyset, \emptyset \rangle$  to  $op_{guard}(S)$  for some set  $S$  of literals. As the operator is effect-less, every infeasible path containing  $n$  remains infeasible. The introduction of  $op_{guard}(S)$  in updates (20) and (21) thus preserves soundness.

Now, suppose the value of  $op[n]$  has been updated from  $\langle \emptyset, \emptyset \rangle$  to  $op_{assert}(GUA_{out}[n], P)$ , for some set  $P$  of propositions. Consider an effect asserted by the auxiliary operator. If the effect is of the form  $?p$ , then it only causes future precondition checks to fail, but never establishes any precondition. If the effect is a literal, and it establishes a precondition, then the precondition is already guaranteed prior to the assertion of the literal. In either case, infeasible paths remain infeasible. Updates (23) and (24) thus preserve soundness.  $\square$

The interface  $\langle pre, post, dead_{in}, dead_{out} \rangle$  of a procedure  $proc$  is said to be **conservative** iff all the following hold: (a)  $pre \subseteq GUA_{in}[n]$  for every call node  $n$  for which  $proc$  is the callee, (b)  $post \subseteq GUA_{in}[n]$  for the exit node  $n$  of  $proc$ , (c)  $dead_{in} \subseteq \Pi \setminus LIV_{out}[n]$  for the entry node  $n$  of  $proc$ , and (d)  $dead_{out} \subseteq \Pi \setminus LIV_{out}[n]$  for every return node  $n$  for which  $proc$  is the callee.

**Theorem 11.** *With conservative interfaces, the revised optimization procedure is transparent and effective.*

*Proof.* If all interfaces are conservative, then the updates (22) and (25) will completely remove the preconditions and effects of the auxiliary operators introduced in (20), (21), (23) and (24).  $\square$

In other words, if the code producer is honest about the optimization directives, all the run-time checks for fraud detection will be optimized away (Theorem 11). However, if the code producer attempts to mislead the code consumer by sending fraudulent procedure interfaces, the fraud will be detected by the IRM at run time (Theorem 10). Lastly, conservative procedure interfaces can be generated by the interface generation algorithm described in Appendix C.

## 6 Accommodating Java-Style Language Constructs

The revised optimization procedure can be further extended to accommodate Java-style exception handling constructs as well as dynamic method dispatching.

## 6.1 Exception Handling

In Appendix A, we provide details on how our optimization procedure can be extended to accommodate Java-style exception handling constructs. As a highlight, procedure interfaces must now assume the form  $\langle pre, post, esc, dead_{in}, dead_{out}, dead_{fail} \rangle$ , where the new components have the following roles:

*esc*: a set of literals guaranteed by the procedure to be established when an exception escapes the procedure

*dead<sub>fail</sub>*: a set of propositions guaranteed to be dead by handlers of exceptions escaping from the procedure

The component *dead<sub>fail</sub>* is introduced to create more opportunities for eliminating effects asserted in normal flow of control. Specifically, if a program is written so that all propositions are always dead on entry to exception handlers, then *dead<sub>fail</sub>* can be set to  $\Pi$ , and opportunities for eliminating effect assertions along normal flow of control will be maximized. The escape-conditions (*esc*) are introduced for symmetry.

## 6.2 Method Overriding

In the presence of dynamic method dispatching, the code consumer must verify that method overriding honors certain constraints among method interfaces. Given method interfaces  $\mathcal{I} = \langle pre, post, esc, dead_{in}, dead_{out}, dead_{fail} \rangle$  and  $\mathcal{I}' = \langle pre', post', esc', dead'_{in}, dead'_{out}, dead'_{fail} \rangle$ , we write  $\mathcal{I}' \sqsubseteq \mathcal{I}$  iff all of the following hold:

$$\begin{array}{lll} pre \supseteq pre' & post \subseteq post' & esc \subseteq esc' \\ dead_{in} \subseteq dead'_{in} & dead_{out} \supseteq dead'_{out} & dead_{fail} \supseteq dead'_{fail} \end{array}$$

The constraints follow the usual contravariant pattern of function subtyping [29]. To preserve safety, the code consumer must verify that  $\mathcal{I}' \sqsubseteq \mathcal{I}$  whenever a method with interface  $\mathcal{I}'$  overrides a method with interface  $\mathcal{I}$ . Since  $\sqsubseteq$  is transitive, only direct method overrides need to be verified. The soundness of this static check follows from the definition of execution traces in the presence of method overriding, the details of which can be found in Appendix B. The interface generation algorithm in Appendix C can be used by the code producer to generate method interfaces guaranteed to satisfy the above static check.

## 7 Implementation Strategy

We developed a Java prototype for the revised optimization procedure (Section 5), with Java bytecode as the target language. Our prototype was developed in Soot [40], a framework for Java bytecode manipulation and optimization. Soot provides facilities for converting Java bytecode into more manageable internal representations, performing control flow analysis to construct control flow graphs, as well as providing infrastructure code for iterative, intraprocedural data flow analyses. Specifically, our prototype consists of three components: (1) a modular optimization procedure, which applies the revised four-step optimization procedure to a CFG and an operator

Name/Version	Description	# classes	# methods
BCEL/5.2	framework for manipulating Java bytecode	384	3184
BcVer/1.0	prints classfile version	11	120
JavaCC/4.0	parser generator	137	2091
JavaTar/2.5	tar-style archiving tool	15	176
ProGuard/4.2	classfile shrinker, optimizer, obfuscater & pre-verifier	447	4211
SableCC/3.2	parser generator	285	2366

Figure 5: Benchmarking suite

assignment, (2) an instrumentation module that converts a CFG and an operator assignment to Java bytecode, and (3) a method interface generator, which is a whole-program analysis built on top of the modular optimization procedure (Appendix C).

Soot’s built-in control flow analyzer has been adopted to construct control flow graphs in the presence of exceptions. Although Soot provides “hooks” for programmers to customize the control flow analyzer so that more accurate exception flows can be obtained, we refrain from following that trail, as precise exception escape analysis is outside of the scope of this work. We however modified the code base of the Soot data flow analysis framework to accommodate the complex data flow equations caused by exception handling.

## 8 Empirical Evaluation

We employed our prototype to empirically assess the degree to which an IRM enforcement mechanism can benefit from the four-step optimization procedure (Section 4), as well as the further improvements brought about by adopting method interfaces as optimization directives in a distributed optimization protocol (Section 5). To benchmark our optimization schemes against production-quality control flow graphs, we selected a suite of open source Java applications for our experiments (see Figure 5). We intentionally consider only batch-processing applications, so that we can fully automate the benchmarking process. For each program, we also select a naturally-occurring input to accompany the program.

To profile the performance of our optimization procedure against history-based access control policies of various structural characteristics, we designed a stochastic procedure for generating benchmarking policies. Given a program  $\mathbb{P}$  and an input  $\mathbb{I}$ , an instance of the **experimental configuration**  $\mathbf{EC}[p_{node}, p_{eff}, p_{pre}]$  (where  $p_{node}$ ,  $p_{eff}$  and  $p_{pre}$  are probabilities) is an operator assignment  $op[\cdot]$  stochastically constructed as follows:

1. Select a set  $N$  of program points from  $\mathbb{P}$  as targets of operator injection. Each program point is selected with probability  $p_{node}$ . Operator assignment  $op[n]$  will remain  $\langle \emptyset, \emptyset \rangle$  for  $n \notin Nodes$ .
2. Fix a set  $\Pi$  of ten propositions. For each  $n \in N$ , set  $op[n]$  to  $\langle \emptyset, eff_n \rangle$ , where each  $eff_n$  is constructed independently as follows: Select a subset  $P$  of  $\Pi$ , such that each  $p \in \Pi$  is selected independently with probability  $p_{eff}$ . Then, construct  $eff_n$  such that, for each  $p \in P$ , with equal probability either  $p$  or  $\neg p$  appears in  $eff_n$ .

3. Instrument  $\mathbb{P}$  with  $op[\cdot]$  and then execute  $\mathbb{P}$  on input  $\mathbb{I}$ . Record the traversed control flow path.
4. For each program point  $n \in N$  that appears on the recorded path, compute the set  $GUA_{in}[n]$  of literals guaranteed to be satisfied at  $n$  during the above execution.
5. For each  $n \in N$ , select a subset  $pre_n$  of literals from  $GUA_{in}[n]$ , such that each member of  $GUA_{in}[n]$  is selected with probability  $p_{pre}$ .
6. Set  $op[n]$  to  $\langle pre_n, eff_n \rangle$  for each  $n \in N$ . This is the operator assignment we seek to construct.

The probability  $p_{node}$  measures *operator density*, while the probabilities  $p_{eff}$  and  $p_{pre}$  measure *effect density* and *precondition density* respectively. The construction procedure guarantees that, on input  $\mathbb{I}$ , program  $\mathbb{P}$  honors the policy represented by  $op[\cdot]$ , and thus benchmarking will not be interrupted by security exceptions.

Given a program  $\mathbb{P}$ , an input  $\mathbb{I}$ , and an operator assignment  $op[\cdot]$ , the effectiveness of an optimization procedure  $\Omega$  is measured as follows. First,  $\mathbb{P}$  is instrumented with  $op[\cdot]$ , and the instrumented program is executed with input  $\mathbb{I}$ . The overhead of execution (as defined in Section 4) is recorded. To better assess the relative effectiveness of precondition and effect elimination, we record the number of preconditions checked as  $O_{pre}^{org}$ , and the number of effects checked as  $O_{eff}^{org}$ . Second, the process is repeated with an optimized operator assignment obtained by applying  $\Omega$  to  $op[\cdot]$ . The overhead of execution as incurred by precondition checks and effect assertions are recorded as  $O_{pre}^{opt}$  and  $O_{eff}^{opt}$ . Optimization effectiveness is then expressed as the ratios  $R_{pre} = 1 - O_{pre}^{opt}/O_{pre}^{org}$  and  $R_{eff} = 1 - O_{eff}^{opt}/O_{eff}^{org}$ . (More effective optimization procedures have larger  $R_{pre}$  and  $R_{eff}$ .)

Our experiments were conducted on an IntelCore 2 Duo 2.33GHz iMac with 2GB of RAM, running Mac OS X 10.4.9, JDK 1.6.0 Update 3, Soot 2.2.5 and Jasmin 2.2.5.

## 8.1 Experiment 1: Optimization With and Without Optimization Directives

In a first experiment, two instantiations of the revised optimization procedure (Section 5) were considered. In the first instantiation, all method interfaces are set to  $\langle \emptyset, \emptyset, \emptyset, \emptyset, \emptyset, \Pi \rangle$ . Adopting an (almost) empty method interface reduces the revised optimization procedure to the basic version reported in Section 4, except that by setting  $dead_{fail}$  to  $\Pi$  we avoid confusing the optimization algorithm with the overly conservative control flow analysis built into Soot for analyzing exception flow. In the second instantiation, we employed the method interface generation algorithm (Appendix C) to generate conservative method interfaces for all methods, and then set  $dead_{fail}$  to  $\Pi$  for the same reason.

We generated ten instances of  $\mathbf{EC}[0.5, 0.5, 0.5]$  for each program in Figure 5, and then measured the optimization effectiveness ratios  $R_{pre}$  and  $R_{eff}$  for each instantiation of the optimization procedure. The measurements for the ten instances were averaged and shown in Figure 6. The bars labeled **pre (empty)** and **eff (empty)** show the average  $R_{pre}$  and  $R_{eff}$  for the optimization procedure with empty method interfaces, while **pre (inferred)** and **eff (inferred)** correspond to average  $R_{pre}$  and  $R_{eff}$  for the optimization procedure with inferred method interfaces.

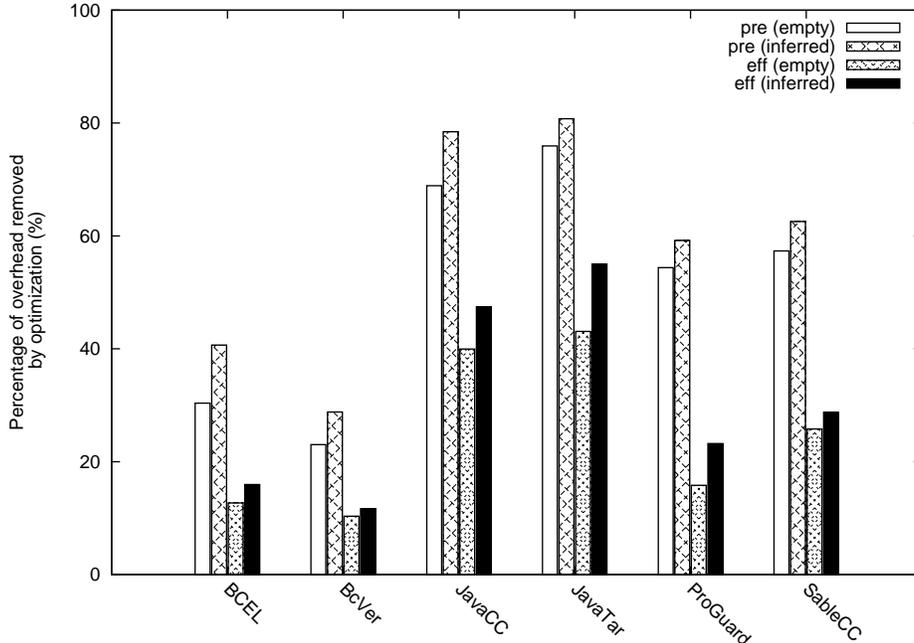


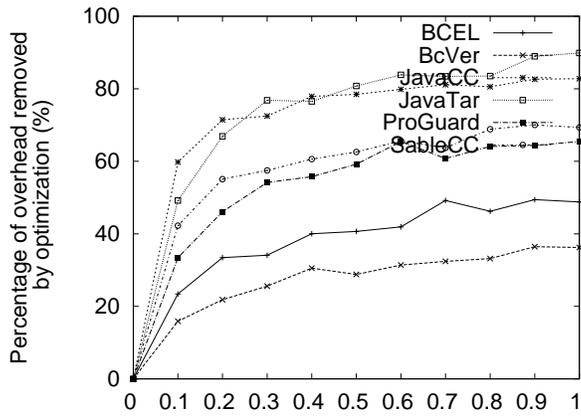
Figure 6: Optimization effectiveness with and without method interfaces.

Three observations can be made from Figure 6. (1) Both precondition and effect elimination deliver significant reduction in performance overhead, even when method interfaces are not present. (2) Precondition elimination has a much higher effectiveness than effect elimination. (3) The added effectiveness of method interfaces is noticeable but not dramatic.

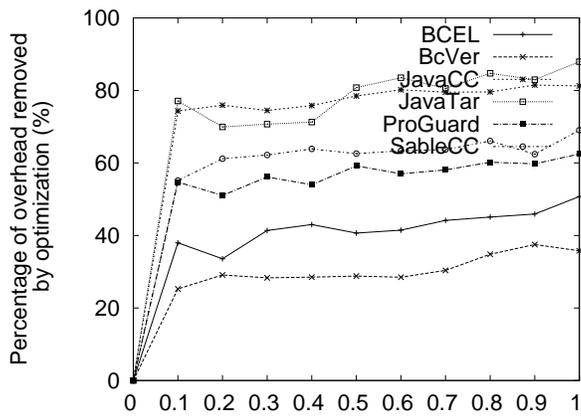
## 8.2 Experiment 2: Varying Policy Characteristics

To characterize optimization effectiveness under various policy structures, we subject the revised optimization procedure (with inferred method interfaces) to different experimental configurations. Specifically, we varied each of  $p_{node}$ ,  $p_{eff}$  and  $p_{pre}$  from 0 to 1, by increments of 0.1, while keeping the other two parameters fixed at 0.5. Again, ten instances of each experimental configuration were generated, and the average effectiveness ratios  $R_{pre}$  and  $R_{eff}$  for each configuration are depicted respectively in Figure 7 and 8.

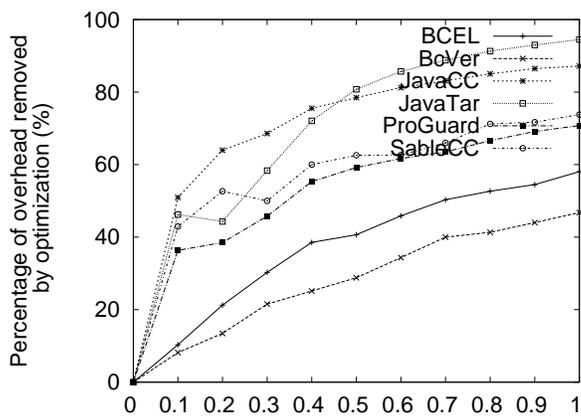
From Figure 8 (a) and (b), we notice that  $R_{eff}$  increases with an increasing effect density ( $p_{eff}$ ), but decreases with an increasing precondition density ( $p_{pre}$ ). We argue that this can be readily explained by data flow equation (8). A higher  $p_{eff}$  increases the size of  $kill_{LIV}[\cdot]$ , creating larger dead sets, and thus promotes effect elimination. A higher  $p_{pre}$ , however, increases the size of  $gen_{LIV}[\cdot]$ , creating smaller dead sets, and thus discourages effect elimination. Similarly, from Figure 7 (a) and (b), we notice that  $R_{pre}$  increases with either an increasing effect density ( $p_{eff}$ ) or an increasing precondition density ( $p_{pre}$ ). This can be explained readily by data flow equation (4), in which larger effect and precondition sets produce larger guaranteed sets, which in turn promote precondition elimination. Notice also that implicit assertion is overridden by explicit assertion, thus explaining why Figure 7 (b) shows a less dramatic increase than Figure 7 (a). The above observations imply that:



(a)

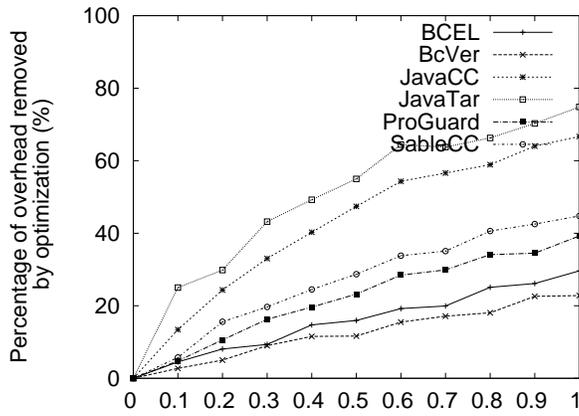


(b)

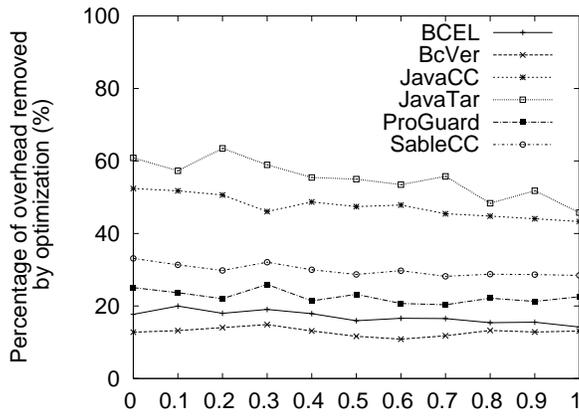


(c)

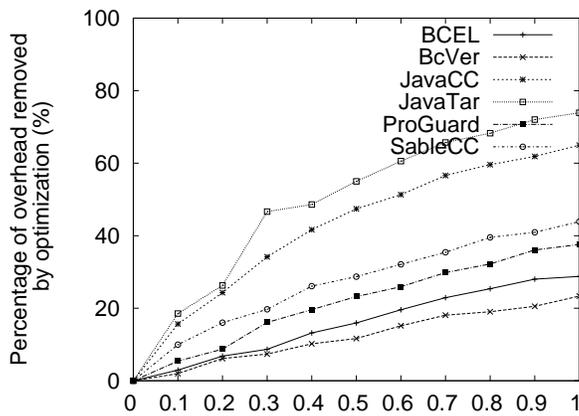
Figure 7:  $R_{pre}$  with different (a)  $p_{eff}$  (b)  $p_{pre}$  (c)  $p_{node}$ .



(a)



(b)



(c)

Figure 8:  $R_{eff}$  with different (a)  $p_{eff}$  (b)  $p_{pre}$  (c)  $p_{node}$ .

*If two different encodings of the same security policy incur similar overhead, then we should prefer the encoding with more effects and less preconditions, for such a policy is more amenable to optimization.*

Figure 7 (c) and 8 (c) show that higher operator density ( $p_{node}$ ) produces higher optimization effectiveness.

*IRM benefits more from precondition and effect elimination when more program points are interpreted as access events.*

## 9 Concluding Remarks

We proposed a constrained policy representation for facilitating IRM optimization. Our policy representation is expressive enough to represent simple integrity policies, Generalized Chinese Wall Policies, and Hierarchical One-Out-Of- $k$  Policies. Our core optimization procedure is sound, transparent and effective. The optimization procedure has been extended to accommodate a distributed optimization protocol, in which an untrusted code producer may formulate method interfaces to boost the optimization effectiveness of a distrusting code consumer. A prototype of the procedure has been implemented, and demonstrated to exhibit positive performance characteristics.

We are exploring alternative optimization directives that could lead to more effective optimization than our current design of method interfaces. While our current policy representation and distributed optimization protocol are designed for supporting control flow policies, we are also exploring how they can be extended to enforce a wider class of security policies.

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## A Exception Handling

### A.1 Program Representation

To accommodate Java-style exception handling, a program is represented as a tuple  $\langle ID, id_{main}, CFG, proc, invoke, interface \rangle$ . Most of the components have the same roles as before, except for the following differences in the representation of control flow graphs ( $CFG$ ) and procedure interfaces ( $interface$ ).

**Control flow graph** A control flow graph (i.e., a member of  $CFG$ ) is a tuple of the following form:

$$\langle N, n_{entry}, n_{exit}, n_{fail}, N_{call}, N_{ret}, N_{hdlr}, N_{instr}, E \rangle$$

- The node set  $N$  is partitioned into seven disjoint subsets:  $\{n_{entry}\}$ ,  $\{n_{exit}\}$ ,  $\{n_{fail}\}$ ,  $N_{call}$ ,  $N_{ret}$ ,  $N_{hdlr}$ , and  $N_{instr}$ . Most of these partitions are now standard. The distinguished **failure node**  $n_{fail}$  represents the program point through which exception escapes from the procedure.  $N_{hdlr}$  is the set of **handler nodes**, each of which represents the entry point of an exception handler.
- A well-formed control flow graph must have an edge set  $E$  that can be uniquely partitioned into four disjoint subsets:  $E_{reg}$ ,  $E_{inv}$ ,  $E_{thr}$  and  $E_{esc}$ . They are respectively the **regular edges**, the **invocation edges**, the **invocation edges**, and the **escape edges**. The partitioning must satisfy the following constraints:

$$\begin{aligned} E_{reg} &\subseteq (N_{instr} \cup N_{ret} \cup N_{hdlr} \cup \{n_{entry}\}) \times (N_{instr} \cup N_{call} \cup \{n_{exit}\}) \\ E_{inv} &\subseteq N_{call} \times N_{ret} \\ E_{thr} &\subseteq N_{instr} \times (N_{hdlr} \cup \{n_{fail}\}) \\ E_{esc} &\subseteq N_{call} \times (N_{hdlr} \cup \{n_{fail}\}) \end{aligned}$$

In addition,  $E_{inv}$  must define a bijection from  $N_{call}$  to  $N_{ret}$ .

**Procedure interfaces** The interface of a procedure takes the form of:

$$\langle pre, post, esc, dead_{in}, dead_{out}, dead_{fail} \rangle$$

The new components have the following role:

$esc$ : a set of literals guaranteed by the procedure to be established at the failure node

$dead_{fail}$ : a set of propositions guaranteed to be dead by the exception handler who catches an exception escaping from the procedure

As a result of introducing these new components, the signature of  $interface$  becomes  $ID \rightarrow (2^{lits(\Pi)} \times 2^{lits(\Pi)} \times 2^{lits(\Pi)} \times 2^\Pi \times 2^\Pi \times 2^\Pi)$ .

**Execution traces** We extend the definition of execution traces in Figure 4 by substituting the following for [LEEP-2]:

[LEEP-2'] a sequence of nodes that can be constructed by applying the following two steps to a  $G$ -local entry path:

- for each invocation edge traversed, insert between the corresponding call node and return node a  $G'$ -local expanded entry path that ends with an exit node, where  $G'$  is the control flow graph of the procedure invoked by that invocation edge
- for each escape edge traversed, insert between the tail and head nodes a  $G'$ -local expanded entry path that ends with a failure node, where  $G'$  is the control flow graph of the procedure invoked by that escape edge

## A.2 Optimization Procedure

The modular optimization procedure expects the following input:

- a control flow graph  $\langle N, n_{entry}, n_{exit}, n_{fail}, N_{call}, N_{ret}, N_{hndlr}, N_{instr}, E \rangle$
- a procedure interface  $\langle pre, post, esc, dead_{in}, dead_{out}, dead_{fail} \rangle$  for the above control flow graph
- a function  $syntbl : N_{call}^* \rightarrow (2^{lits(\Pi)} \times 2^{lits(\Pi)} \times 2^{lits(\Pi)} \times 2^\Pi \times 2^\Pi \times 2^\Pi)$  that maps each call node to the procedure interface of the callee (i.e.,  $syntbl(n)$  is a shorthand for  $interface[invoke[n]]$ )
- an operator assignment  $op[\cdot]$  that maps each node to an operator, so that  $op[n] = \langle \emptyset, \emptyset \rangle$  if  $n \notin N_{instr}$

The optimization procedure proceeds as follows.

### Step 1 - guaranteed set analysis

$$\begin{aligned}
GUA_{in}[n] &= \bigcap_{m \in pred[n]} GUA_{out}[m] && \text{for } n \in N_{instr} \cup N_{call} \cup \{n_{exit}\} \\
GUA_{in}[n] &= \bigcap_{m \in pred[n]} GUA_{fail}[m] && \text{for } n \in N_{hndlr} \cup \{n_{fail}\} \\
GUA_{out}[n] &= pre && \text{for } n \in \{n_{entry}\} \\
GUA_{out}[n] &= syntbl(E_{inv}^{-1}(n)).post && \text{for } n \in N_{ret} \\
GUA_{out}[n] &= (GUA_{in}[n] \oplus op[n].pre) \oplus op[n].eff && \text{for } n \in N_{instr} \\
GUA_{out}[n] &= GUA_{in}[n] && \text{for } n \in N_{hndlr} \\
GUA_{fail}[n] &= GUA_{in}[n] \oplus op[n].pre && \text{for } n \in N_{instr} \\
GUA_{fail}[n] &= syntbl(n).esc && \text{for } n \in N_{call}
\end{aligned}$$

**Step 2 - precondition elimination** First, introduce the following auxiliary operators:

$$\begin{aligned}
op[n] &:= op_{guard}(symtbl(n).pre) && \text{for } n \in N_{call} \\
op[n] &:= op_{guard}(post) && \text{for } n \in \{n_{exit}\} \\
op[n] &:= op_{guard}(esc) && \text{for } n \in \{n_{fail}\}
\end{aligned}$$

Second, eliminate preconditions:

$$op[n].pre := op[n].pre \setminus \text{GUA}_{in}[n] \quad \text{for } n \in N_{instr} \cup N_{call} \cup \{n_{exit}\} \cup \{n_{fail}\}$$

**Step 3 - liveness analysis**

$$\text{LIV}_{out}[n] = \bigcup_{m \in succ[n \mid E_{reg}]} \text{LIV}_{in}[m] \quad \text{for } n \in N_{instr} \cup N_{ret} \cup N_{hdlr} \cup \{n_{entry}\}$$

$$\text{LIV}_{fail}[n] = \bigcup_{m \in succ[n \mid E_{thr} \cup E_{esc}]} \text{LIV}_{in}[m] \quad \text{for } n \in N_{instr} \cup N_{call}$$

$$\begin{aligned} \text{LIV}_{in}[n] &= ((\text{LIV}_{out}[n] \setminus kill_{\text{LIV}}[n]) \cup gen_{\text{LIV}}[n]) \\ &\quad \cup (\text{LIV}_{fail}[n] \cup gen_{\text{LIV}}[n]) \end{aligned} \quad \text{for } n \in N_{instr}$$

$$\text{LIV}_{in}[n] = \text{LIV}_{out}[n] \quad \text{for } n \in N_{hdlr}$$

$$\text{LIV}_{in}[n] = (\Pi \setminus symtbl(n).dead_{in}) \cup vars(op[n].pre) \quad \text{for } n \in N_{call}$$

$$\text{LIV}_{in}[n] = (\Pi \setminus dead_{out}) \cup vars(op[n].pre) \quad \text{for } n \in \{n_{exit}\}$$

$$\text{LIV}_{in}[n] = (\Pi \setminus dead_{fail}) \cup vars(op[n].pre) \quad \text{for } n \in \{n_{fail}\}$$

**Step 4 - effect elimination** First, introduce the following auxiliary operators:

$$\begin{aligned}
op[n] &:= op_{assert}(\text{GUA}_{out}[n], dead_{in}) && \text{for } n \in \{n_{entry}\} \\
op[n] &:= op_{assert}(\text{GUA}_{out}[n], symtbl(E_{inv}^{-1}(n)).dead_{out}) && \text{for } n \in N_{ret} \\
op[n] &:= op_{assert}(\text{GUA}_{out}[n], D[n]) && \text{for } n \in N_{hdlr}
\end{aligned}$$

where

$$D[n] = \bigcup_{m \in pred[m \mid E_{esc}]} symtbl(m).dead_{fail}$$

Second, eliminate effects as follows:

$$op[n].eff := op[n].eff \cap \text{LIV}_{out}[n] \quad \text{for } n \in N_{instr} \cup N_{ret} \cup N_{hdlr} \cup \{n_{entry}\}$$

## B Program Representation with Method Overriding

As in every other modern object-oriented programming platforms, the Java language supports dynamic method dispatching. This feature slightly complicates the treatment of procedure/method invocations (from now on we use the word “procedure” and “method” interchangeably). Specifically, a program is represented as follows:

$$\langle ID, id_{main}, overrides, CFG, proc, invoke, interface \rangle$$

- The binary relation  $overrides \subseteq ID \times ID$  is a partial ordering of procedure identifiers, modeling method overriding. Specifically, we write  $overrides(id_1, id_2)$  if  $id_1$  overrides  $id_2$ . Note that, as  $overrides$  is reflexive, every procedure identifier overrides itself by definition.
- The mapping  $proc$  is a partial function, meaning that some procedure ids are not assigned a control flow graph (abstract method do not have bodies). It is understood that the main procedure does have a body. It is also understood that, at run time, any one of the control flow graphs overriding the procedure identifier named at a call site may be dispatched non-deterministically.

The definition of execution traces in Figure 4 is extended by substituting the following for **[LEEP-2]** and **[LEEP-3]**:

**[LEEP-2'']** a sequence of nodes that can be constructed by applying the following two steps to a  $G$ -local entry path:

- for each invocation edge traversed, insert between the corresponding call node and return node a  $G'$ -local expanded entry path that ends with an exit node, where  $G'$  is the control flow graph of a method overriding the method signature invoked by that invocation edge (because  $overrides$  is reflexive, the two methods may be identical)
- for each escape edge traversed, insert between the tail and head nodes a  $G'$ -local expanded entry path that ends with a failure node, where  $G'$  is the control flow graph of a method overriding the method signature invoked by that escape edge

**[LEEP-3'']** a path that can be constructed by concatenating the following two sequences: (i) a  $G$ -local expanded entry path ending with a call node for method signature  $id$ , and (ii) a  $G'$ -local expanded entry path, where  $G'$  is the control flow graph of a method overriding the method signature invoked by the call node.

## C Generating Method Interfaces

This appendix describes a whole-program analysis that computes method interfaces for program representations involving procedure interfaces (Section 5.2), exceptions (Appendix A) and method overriding (Section B). To fix thoughts, we assume the program representation described in Appendix B, which subsumes all the preceding program representations.

The basic idea of the whole-program analysis (see below for full listing) is that, we begin with assigning to each method signature an overly conservative method interface (i.e., all interface components are empty sets), and then conduct two whole-program data flow analyses to incrementally improve the accuracy of the interfaces. The first whole-program analysis computes the interface components  $pre$ ,  $post$  and  $esc$  for each method, and the second computes the  $dead_{in}$ ,  $dead_{out}$  and  $dead_{fail}$  components. Each whole-program analysis is a standard work-list algorithm: the work list tracks which method needs processing. In each iteration, the work-list algorithm examines one method, and invokes one of the intraprocedural analyses (i.e., **Step 1** and **Step 3** of the optimization procedure in Section A) as a subroutine.

The algorithm tracks two associative arrays:  $GUA^*[\cdot]$  and  $LIV^*[\cdot]$ . The mapping  $GUA^*[\cdot]$  assigns a conservative guaranteed set to each node in  $N_{call}^* \cup N_{exit}^* \cup N_{fail}^*$ . Specifically,  $GUA^*[\cdot]$  tracks the

$GUA_{in}[\cdot]$  values of call, exit and failure nodes. The guaranteed set components (i.e., *pre*, *post* and *esc*) of the inferred method interfaces are computed from the elements of this associative array. Every time the intraprocedural guaranteed set analysis (i.e., **Step 1**) is invoked, the estimates in  $GUA^*[\cdot]$  are improved. The improved estimates are then employed to improve the guaranteed set components of the method interfaces. The improvements in method interfaces then induce further improvements in the accuracy of the intraprocedural guaranteed set analyses. The process terminates when the estimates stabilize. Similarly, the mapping  $LIV^*[\cdot]$  tracks the  $LIV_{out}[\cdot]$  values of return and entry nodes, as well as the  $LIV_{fail}[\cdot]$  values of call nodes. The dead set components (i.e.,  $dead_{in}$ ,  $dead_{out}$  and  $dead_{fail}$ ) of the inferred method interfaces are computed from the elements of these live sets. As in the previous case, each invocation of the intraprocedural liveness analysis (i.e., **Step 3**) improves the estimates in  $LIV^*[\cdot]$ , thereby producing improved method interfaces. This in turn yields a more accurate intraprocedural liveness analysis. Again, the process terminates when the values stabilize.

The method interfaces inferred by the algorithm are constructed to be both conservative (Section 5.4) and compliant to the method overriding constraints (Appendix B). For instance, the *pre* component of the method interface for a method  $id$  is set to  $\bigcap_{m \in C} GUA^*[m]$ , where  $C = \{m \in N_{call}^* \mid overrides(id, invoke[m])\}$ . In other words, a literal is in the *pre* component of  $id$  iff it is in  $GUA^*[m]$  for all call sites  $m$  of either  $id$  or any of the methods it overrides. The other method interface components are constructed in a similarly conservative manner.

In the following, the domain of a partial function  $f$  is denoted by  $dom(f)$ .

**Step 1** Initialize method interfaces.

```

for  $id \in ID$  do
   $interface[id] := \langle \emptyset, \emptyset, \emptyset, \emptyset, \emptyset, \emptyset \rangle;$ 

```

**Step 2** Compute guaranteed set components (i.e., *pre*, *post* and *esc*).

```

for  $n \in N_{call}^* \cup N_{exit}^* \cup N_{fail}^*$  do
   $GUA^*[n] := \emptyset;$ 
   $WL := dom(proc);$ 
  while  $WL \neq \emptyset$  do
    /* Extract next procedure from work list */
    select  $id \in WL;$ 
     $WL := WL \setminus \{id\};$ 
    /* Compute guaranteed sets */
    run Step 1 of the optimization procedure in Section A on  $proc[id];$ 
    let  $GUA_{in}[\cdot]$  be the guaranteed sets computed by that step;
    /* Propagate guaranteed sets of  $N_{call}$  */
    for  $n \in proc[id].N_{call}$  do
      if  $GUA^*[n] \neq GUA_{in}[n]$  then
         $GUA^*[n] := GUA_{in}[n];$ 
        for  $id' \in ID$  such that  $overrides(id', invoke[n])$  do
          let
             $C = \{m \in N_{call}^* \mid overrides(id', invoke[m])\};$ 

```

```

     $G = \bigcap_{m \in C} \text{GUA}^*[m];$ 
in
    if  $\text{interface}[id'].pre \neq G$  then
         $\text{interface}[id'].pre := G;$ 
        if  $id' \in \text{dom}(\text{proc})$  then
             $WL := WL \cup \{id'\};$ 
    /* Propagate guaranteed set of  $n_{exit}$  */
let
     $n = \text{proc}[id].n_{exit};$ 
in
    if  $\text{GUA}^*[n] \neq \text{GUA}_{in}[n]$  then
         $\text{GUA}^*[n] := \text{GUA}_{in}[n];$ 
        for  $id' \in ID$  such that  $\text{overrides}(id, id')$  do
            let
                 $E = \{ \text{proc}[id''].n_{exit} \mid id'' \in ID \text{ such that } \text{overrides}(id'', id') \};$ 
                 $G = \bigcap_{m \in E} \text{GUA}^*[m];$ 
            in
                if  $\text{interface}[id'].post \neq G$  then
                     $\text{interface}[id'].post := G;$ 
                    if  $id' \in \text{dom}(\text{proc})$  then
                         $WL := WL \cup \{id'\};$ 
            /* Propagate guaranteed set of  $n_{fail}$  */
            let
                 $n = \text{proc}[id].n_{fail};$ 
            in
                if  $\text{GUA}^*[n] \neq \text{GUA}_{in}[n]$  then
                     $\text{GUA}^*[n] := \text{GUA}_{in}[n];$ 
                    for  $id' \in ID$  such that  $\text{overrides}(id, id')$  do
                        let
                             $F = \{ \text{proc}[id''].n_{fail} \mid id'' \in ID \text{ such that } \text{overrides}(id'', id') \};$ 
                             $G = \bigcap_{m \in F} \text{GUA}^*[m];$ 
                        in
                            if  $\text{interface}[id'].esc \neq G$  then
                                 $\text{interface}[id'].esc := G;$ 
                                if  $id' \in \text{dom}(\text{proc})$  then
                                     $WL := WL \cup \{id'\};$ 

```

**Step 3** Compute dead set components (i.e.,  $dead_{in}$ ,  $dead_{out}$  and  $dead_{fail}$ ).

```

for  $n \in N_{ret}^* \cup N_{call}^* \cup N_{entry}^*$  do
     $\text{LIV}^*[n] := \Pi;$ 
     $WL := \text{dom}(\text{proc});$ 
while  $WL \neq \emptyset$  do
    /* Extract next procedure from work list */
    select  $id \in WL;$ 

```

```

WL := WL \ {id};
/* Compute live sets */
run Step 3 of the optimization procedure in Section A on  $proc[id]$ ;
let  $LIV_{out}[\cdot]$  and  $LIV_{fail}[\cdot]$  be the live sets computed by that step;
/* Propagate live sets of  $N_{ret}$  */
for  $n \in proc[id].N_{ret}$  do
  if  $LIV^*[n] \neq LIV_{out}[n]$  then
     $LIV^*[n] := LIV_{out}[n]$ ;
    for  $id' \in ID$  such that  $overrides(id', invoke[(E_{inv}^*)^{-1}(n)])$  do
      let
         $R = \{m \in N_{ret}^* \mid overrides(id', invoke[(E_{inv}^*)^{-1}(m)])\}$ ;
         $D = \Pi \setminus \bigcup_{m \in R} LIV^*[m]$ ;
      in
        if  $interface[id'].dead_{out} \neq D$  then
           $interface[id'].dead_{out} := D$ ;
          if  $id' \in dom(proc)$  then
             $WL := WL \cup \{id'\}$ ;
/* Propagate live sets at the "failure port" of  $N_{call}$  */
for  $n \in proc[id].N_{call}$  do
  if  $LIV^*[n] \neq LIV_{fail}[n]$  then
     $LIV^*[n] := LIV_{fail}[n]$ ;
    for  $id' \in ID$  such that  $overrides(id', invoke[n])$  do
      let
         $C = \{m \in N_{call}^* \mid overrides(id', invoke[m])\}$ ;
         $D = \Pi \setminus \bigcup_{m \in C} LIV^*[m]$ ;
      in
        if  $interface[id'].dead_{fail} \neq D$  then
           $interface[id'].dead_{fail} := D$ ;
          if  $id' \in dom(proc)$  then
             $WL := WL \cup \{id'\}$ ;
/* Propagate live set of  $n_{entry}$  */
let
   $n = proc[id].n_{entry}$ ;
in
  if  $LIV^*[n] \neq LIV_{out}[n]$  then
     $LIV^*[n] := LIV_{out}[n]$ ;
    for  $id' \in ID$  such that  $overrides(id, id')$  do
      let
         $E = \{proc[id''].n_{entry} \mid id'' \in ID \text{ such that } overrides(id'', id')\}$ ;
         $D = \Pi \setminus \bigcup_{m \in E} LIV^*[m]$ ;
      in
        if  $interface[id'].dead_{in} \neq D$  then
           $interface[id'].dead_{in} := D$ ;
          if  $id' \in dom(proc)$  then
             $WL := WL \cup \{id'\}$ ;

```