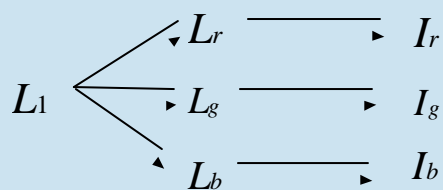


Lighting and Shading

Shading - recap

- Adding colour



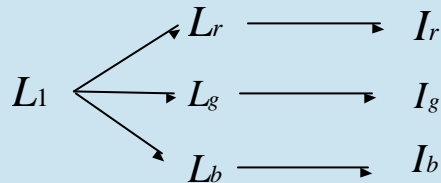
$$I_r = K_{ar}L_{ar} + K_{dr}(l \cdot n)L_{dr} + K_{sr}(r \cdot v)^{a_r}$$
$$I_g = K_{ag}L_{ag} + K_{dg}(l \cdot n)L_{dg} + K_{sg}(r \cdot v)^{a_g}$$
$$I_b = K_{ab}L_{ab} + K_{db}(l \cdot n)L_{db} + K_{sb}(r \cdot v)^{a_b}$$

- Combine

$$I_r + I_g + I_b$$

Shading - recap

- Adding colour



$$I_r = K_{ar}L_{ar} + K_{dr}(l \cdot n)L_{dr} + K_{sr}(r \cdot v)^{a_r}$$

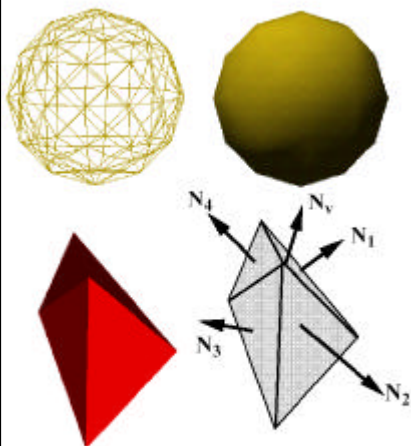
$$I_g = K_{ag}L_{ag} + K_{dg}(l \cdot n)L_{dg} + K_{sg}(r \cdot v)^{a_g}$$

$$I_b = K_{ab}L_{ab} + K_{db}(l \cdot n)L_{db} + K_{sb}(r \cdot v)^{a_b}$$

- Combine

$$I_r + I_g + I_b$$

Gouraud Shading (intensity interpolation)



Averaged Normal N_v is

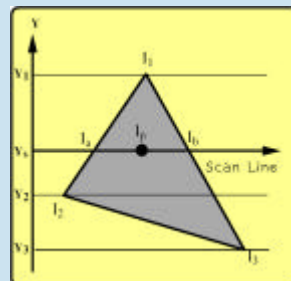
$$\frac{\sum N_i}{|\sum N_i|}$$

Intensity interpolation along each scan line and along polygon edges:

$$I_a = I_1 - (I_1 - I_2) \frac{Y_1 - Y_s}{Y_1 - Y_2}$$

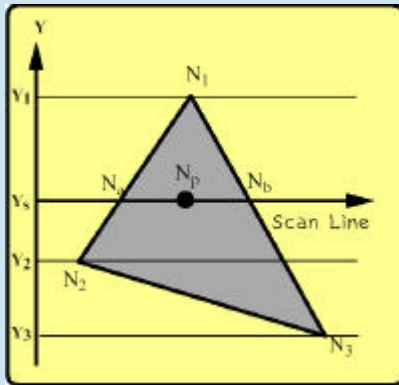
$$I_b = I_1 - (I_1 - I_3) \frac{Y_1 - Y_s}{Y_1 - Y_3}$$

$$I_p = I_b - (I_b - I_a) \frac{X_b - X_p}{X_b - X_a}$$



Phong Shading (normal vector interpolation)

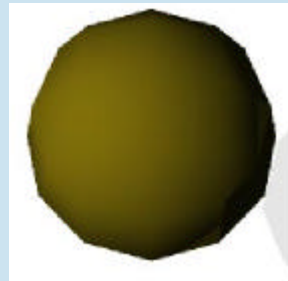
- Normal vector interpolation along each edge and each scan line



$$N_a = N_1 - (N_1 - N_2) \frac{Y_1 - Y_s}{Y_1 - Y_2}$$

$$N_b = N_1 - (N_1 - N_3) \frac{Y_1 - Y_s}{Y_1 - Y_3}$$

$$N_p = N_b - (N_b - N_a) \frac{X_b - X_p}{X_b - X_a}$$



Shading comparisons

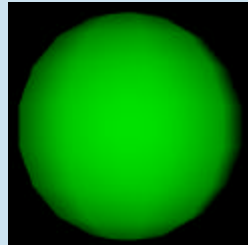
Flat

- single colour to each polygon
- fast
- faceted look



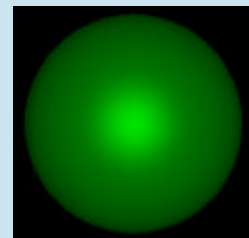
Gouraud

- intensity interpolation
- smoother effect
- some mach banding
- specular highlights handled poorly
- more computation



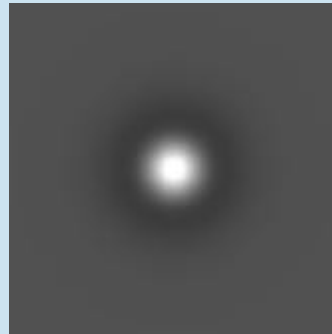
Phong

- vector normal interpolation
- more accurate
- more realistic highlights
- much less Mach banding
- much more computation



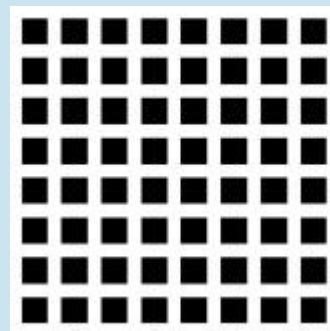
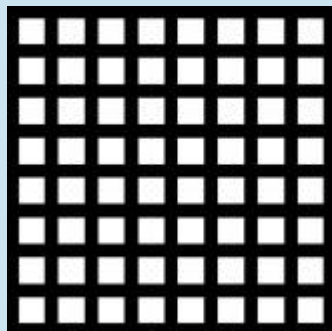
Human Perception and Light

- Difference Signaling
 - Contrast vs. value information
 - Light value information vs. object information.
- cell has normal rate
 - light in centre excites
 - light in surrounds inhibits
- Colour and Lightness Constancy



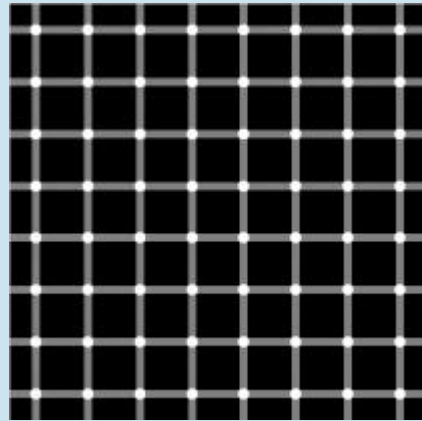
Consequences

- Hermann Grid Illusion



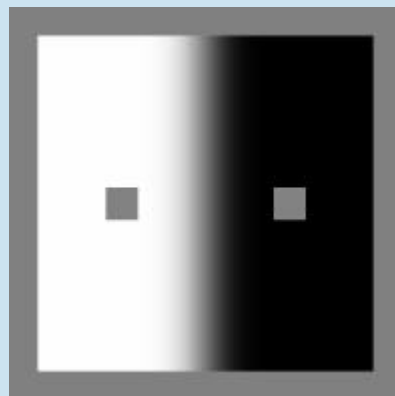
Consequences

- Scintillating Grid



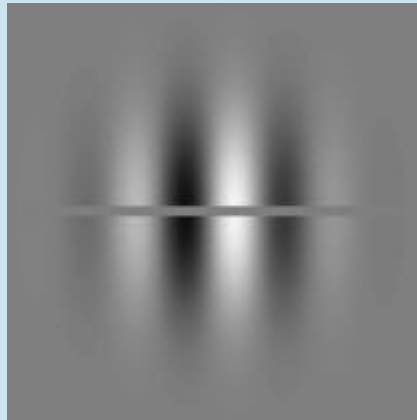
Consequences

- Simultaneous Brightness Contrast



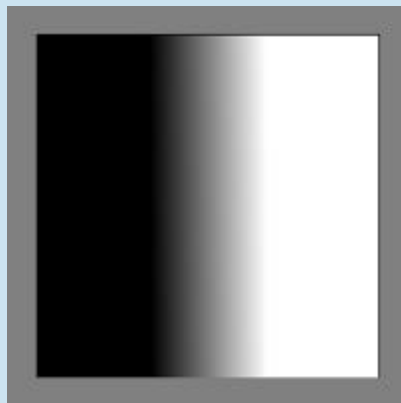
Consequences

- Grating Induction Effect



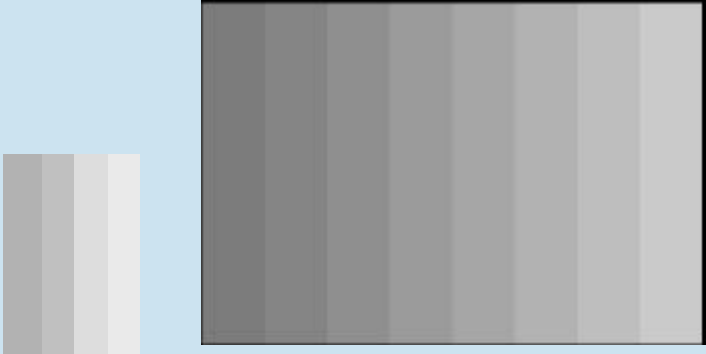
Consequences

- Mach Banding



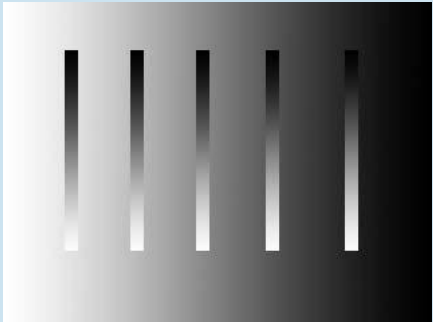
Consequences

- Chevreul Illusion



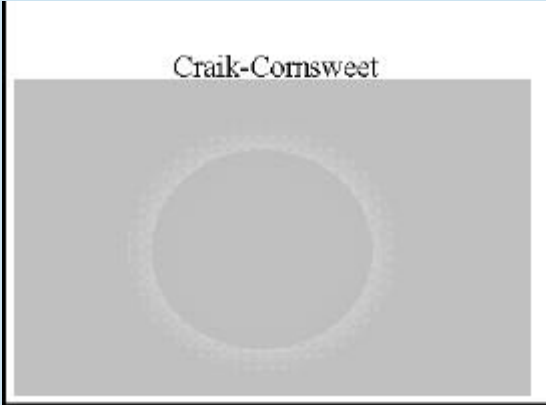
Consequences

- Crispening



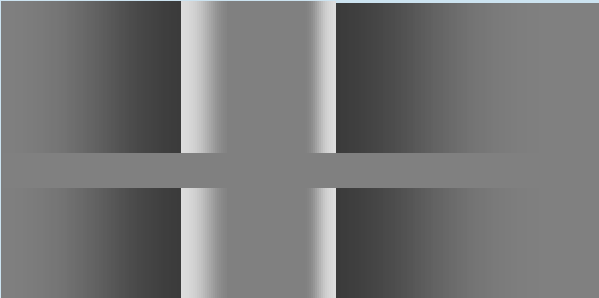
Consequences

- Craik-Cornsweet Effect



Consequences

- Craik-Cornsweet Effect

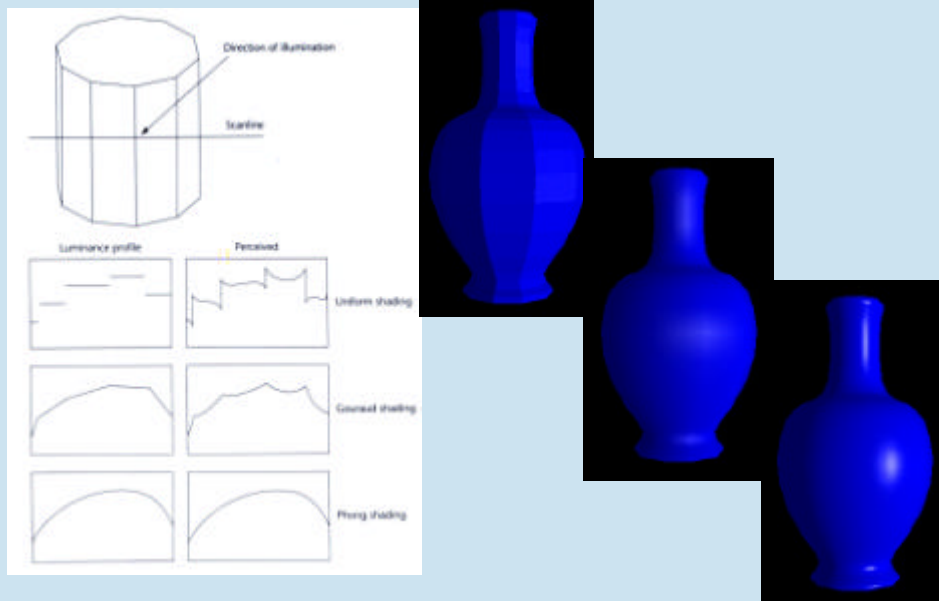


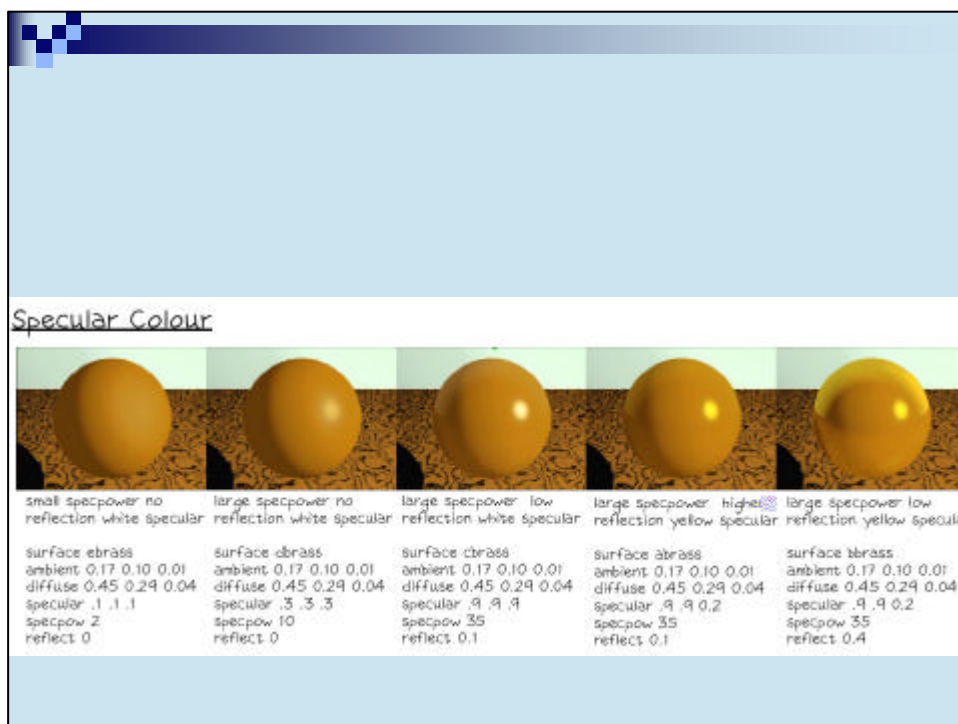
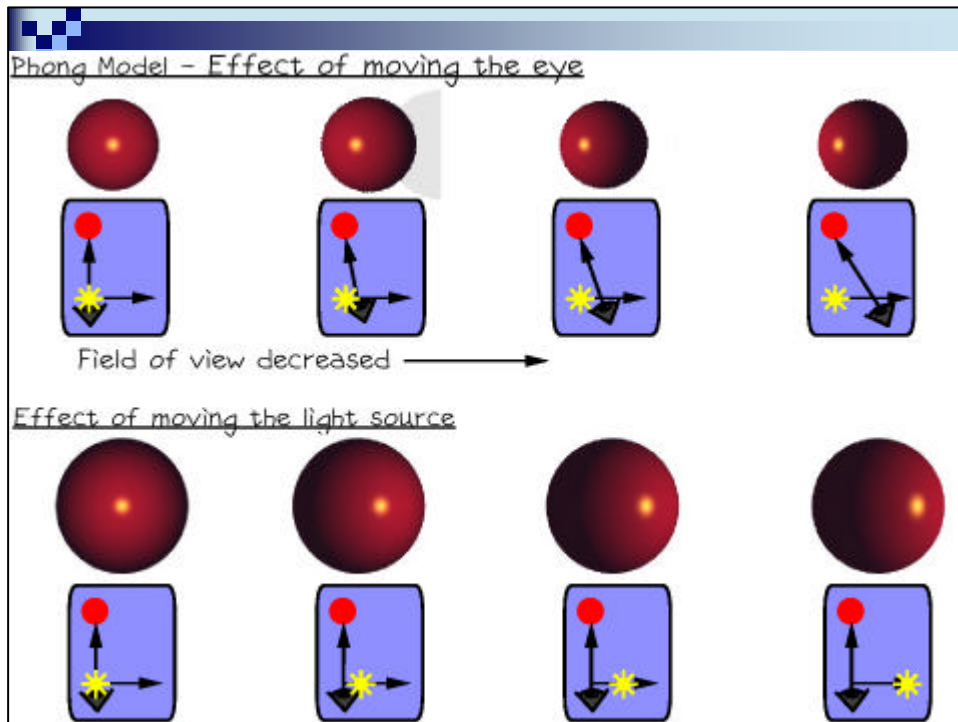
Seurat: The Bathers

- Craik-Cornsweet Effect

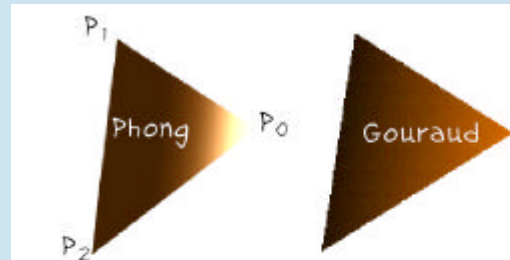


Shading Comparisons





More on Phong shading



The normal vectors have been adjusted to give a highlight at P_0 but not at the other vertices. In the Gouraud interpolation scheme the highlight is lost, averaged out with the other vertex intensities. The Phong interpolation finds the correct highlight.

Problems with interpolation methods

- **Expensive:** since illumination calculation is repeated for every pixel. Also calculating and normalising new normal. (Schlick equation and table look up methods).
- **Silhouette edge:** Attempts have been made to modify normals to match a curve fitted to the edge. (see Van Overveld and Wyvill)
- **Perspective distortion:** Intensity interpolation is performed in screen space. The z has undergone a non-linear transformation.



Problems with interpolation methods

- **Orientation Dependence:** The results of an interpolation model are not independent of the projected polygons orientation. Results may differ when the polygon is rotated affecting animations.
- **Problems at Shared Vertices:** This problem is analagous to the cracks problem in subdivided meshes. The undivided edge is interpolated differently to the two divided edges.
- **Unrepresentative Vertex Normals:** Pathological cases where interpolated normals give poor results. Examples are staircase example and mobius strip.