## Resolution in Prepositional Logic Examples

$$s_0 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s, \neg s \lor p, p \lor \neg r\}$$



# $s_0 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s, \neg s \lor p, p \lor \neg r\}$ $\neg s \lor p$ can be subsumed into $\neg s$

$$s_0 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s, \neg s \lor p, p \lor \neg r\}$$
  
 $\neg s \lor p$  can be subsumed into  $\neg s$ 

$$S_0 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s, \neg s \lor p, p \lor \neg r\}$$

¬s∨p can be subsumed into ¬s

$$S_0 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s, \neg s \lor p, p \lor \neg r\}$$

# Resolution between ¬p∨s and ¬s

$$s_0 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s, \neg s \lor p, p \lor \neg r\}$$

#### ¬s∨p can be subsumed into ¬s Resolution between ¬p∨s and ¬s

# s₀ = {r∨p∨s, s∨q, ¬p∨s, ¬s, ¬s∨p, p∨¬r}

#### ¬s∨p can be subsumed into ¬s Resolution between ¬p∨s and ¬s

#### ¬s∨p can be subsumed into ¬s Resolution between ¬p∨s and ¬s Resolution between s∨q and ¬s

#### ¬s∨p can be subsumed into ¬s Resolution between pys and ¬s Resolution between s∨q and ¬s

## s₀ = {r∨p∨s, s∨q, ¬p∨s, ¬s, ¬s∨p, p∨¬r} ¬s∨p can be subsumed into ¬s Resolution between ¬p∨s and ¬s Resolution between s∨q and ¬s

## s₀ = {r∨p∨s, s∨q, ¬p∨s, ¬s, ¬s∨p, p∨¬r} ¬s∨p can be subsumed into ¬s Resolution between ¬p∨s and ¬s Resolution between s∨q and ¬s

 $s_0 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s \lor p, p \lor \neg r\}$ ¬s∨p can be subsumed into ¬s Resolution between  $p_{\gamma}$  and  $\neg$ s Resolution between  $s\sqrt{q}$  and  $\neg s$ Resolution between  $r \vee p \vee s$  and  $\neg s$ 

#### ¬s∨p can be subsumed into ¬s Resolution between ¬p∨s and ¬s Resolution between s∨q and ¬s Resolution between r∨p∨s and ¬s

$$f_{wert,1}(\{\neg s, \neg s \lor p\}, \{\neg s\}) = 0$$

#### ¬s∨p can be subsumed into ¬s Resolution between ¬p∨s and ¬s Resolution between s∨q and ¬s Resolution between r∨p∨s and ¬s

$$f_{wert,1}(\{\neg s, \neg s \lor p\}, \{\neg s\}) = 0$$
  
$$f_{wert,1}(\{s \lor q, \neg s\}, \{s \lor q, \neg s, q\}) = 1$$

¬s∨p can be subsumed into ¬s Resolution between ¬p∨s and ¬s Resolution between s∨q and ¬s Resolution between r∨p∨s and ¬s

$$\begin{split} f_{wert,1}(\{\neg s, \neg s \lor p\}, \{\neg s\}) &= 0 \\ f_{wert,1}(\{s \lor q, \neg s\}, \{s \lor q, \neg s, q\}) &= 1 \\ f_{wert,1}(\{\neg p \lor s, \neg s\}, \{\neg p \lor s, \neg s, \neg p\}) &= 1 \end{split}$$

¬s∨p can be subsumed into ¬s Resolution between ¬p∨s and ¬s Resolution between s∨q and ¬s Resolution between r∨p∨s and ¬s

$$\begin{split} f_{wert,1}(\{\neg s, \neg s \lor p\}, \{\neg s\}) &= 0 \\ f_{wert,1}(\{s \lor q, \neg s\}, \{s \lor q, \neg s, q\}) &= 1 \\ f_{wert,1}(\{\neg p \lor s, \neg s\}, \{\neg p \lor s, \neg s, \neg p\}) &= 1 \\ f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) &= 2 \end{split}$$

$$S_0 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s, \neg s \lor p, p \lor \neg r\}$$

#### ¬s∨p can be subsumed into ¬s Resolution between ¬p∨s and ¬s Resolution between s∨q and ¬s Resolution between r∨p∨s and ¬s

 $\begin{aligned} f_{wert,1}(\{s \lor q, \neg s\}, \{s \lor q, \neg s, q\}) &= 1 \\ f_{wert,1}(\{\neg p \lor s, \neg s\}, \{\neg p \lor s, \neg s, \neg p\}) &= 1 \end{aligned}$ 

 $f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2$ 

# $s_{0} = \{r \lor p \lor s, \ s \lor q, \ \neg p \lor s, \ \neg s, \ \neg s \lor p, \ p \lor \neg r\}$ $\downarrow$ $s_{1} = \{r \lor p \lor s, \ s \lor q, \ \neg p \lor s, \ \neg s, \ p \lor \neg r\}$

Resolution between ¬p∨s and ¬s Resolution between s∨q and ¬s Resolution between r∨p∨s and ¬s

$$\begin{split} f_{wert,1}(\{s \lor q, \neg s\}, \{s \lor q, \neg s, q\}) &= 1 \\ f_{wert,1}(\{\neg p \lor s, \neg s\}, \{\neg p \lor s, \neg s, \neg p\}) &= 1 \\ f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) &= 2 \end{split}$$

Resolution between ¬p∨s and ¬s Resolution between s∨q and ¬s Resolution between r∨p∨s and ¬s

$$\begin{aligned} & f_{wert,1}(\{s \lor q, \neg s\}, \{s \lor q, \neg s, q\}) = 1 \\ & f_{wert,1}(\{\neg p \lor s, \neg s\}, \{\neg p \lor s, \neg s, \neg p\}) = 1 \\ & f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \end{aligned}$$

# $s_{1} = \{r \lor p \lor s, \ s \lor q, \ \neg p \lor s, \ \neg s, \ \neg s \lor p, \ p \lor \neg r\}$ $\downarrow$ $s_{2} = \{r \lor p \lor s, \ s \lor q, \ \neg p \lor s, \ \neg s, \ p \lor \neg r, \ q\}$

#### Resolution between ¬p∨s and ¬s Resolution between r∨p∨s and ¬s

 $s_2 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s, p \lor \neg r, q\}$ 

#### Resolution between ¬p∨s and ¬s Resolution between r∨p∨s and ¬s

 $s_2 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s, p \lor \neg r, q\}$ 

#### Resolution between ¬p∨s and ¬s Resolution between r∨p∨s and ¬s

#### Resolution between ¬p∨s and ¬s Resolution between r∨p∨s and ¬s

#### Resolution between ¬p∨s and ¬s Resolution between r∨p∨s and ¬s s∨q can be subsumed into q

Resolution between ¬p∨s and ¬s Resolution between r∨p∨s and ¬s s∨q can be subsumed into q

$$\begin{split} f_{wert,1}(\{q, s \lor q\}, \{q\}) &= 0 \\ f_{wert,1}(\{\neg p \lor s, \neg s\}, \{\neg p \lor s, \neg s, \neg p\}) &= 1 \\ f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) &= 2 \end{split}$$

#### Resolution between ¬p∨s and ¬s Resolution between r∨p∨s and ¬s s∨q can be subsumed into q

$$\begin{split} f_{wert,1}(\{q, s \lor q\}, \{q\}) &= 0 \\ f_{wert,1}(\{\neg p \lor s, \neg s\}, \{\neg p \lor s, \neg s, \neg p\}) &= 1 \\ f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) &= 2 \end{split}$$
## $s_2 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s, p \lor \neg r, q\}$

#### $s_2 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s, p \lor \neg r, q\}$

#### $s_2 = \{r \lor p \lor s, s \lor q, \neg p \lor s, \neg s, p \lor \neg r, q\}$

#### $s_3 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q\}$

 $S_3 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q\}$ 

#### Resolution between ¬p∨s and ¬s Resolution between r∨p∨s and ¬s

# $$\begin{split} f_{wert,1}(\{\neg p \lor s, \neg s\}, \{\neg p \lor s, \neg s, \neg p\}) &= 1 \\ f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) &= 2 \end{split}$$

 $S_3 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q\}$ 

### Resolution between ¬p∨s and ¬s Resolution between r∨p∨s and ¬s

$$\begin{aligned} &f_{wert,1}(\{\neg p \lor s, \neg s\}, \{\neg p \lor s, \neg s, \neg p\}) = 1 \\ &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \end{aligned}$$

#### $S_3 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q\}$

#### $S_3 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q\}$

#### $s_3 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q\}$

#### $S_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$

## $s_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$ Resolution between $r \lor p \lor s$ and $\neg s$

#### Resolution between $r \lor p \lor s$ and $\neg s$

$$s_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$$

#### Resolution between r∨p∨s and ¬s

$$s_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$$
  
Resolution between  $r \lor p \lor s$  and  $\neg s$ 

$$s_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$$
  
Resolution between  $r \lor p \lor s$  and  $\neg s$   
Resolution between  $p \lor \neg r$  and  $\neg p$ 

## Resolution between $r \lor p \lor s$ and $\neg s$ Resolution between $p \lor \neg r$ and $\neg p$

$$s_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$$
  
Resolution between  $r \lor p \lor s$  and  $\neg s$   
Resolution between  $p \lor \neg r$  and  $\neg p$ 

## $s_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$ Resolution between $r \lor p \lor s$ and $\neg s$ Resolution between $p \lor \neg r$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg p$

## s₄ = {r∨p∨s, ¬p∨s, ¬s, p∨¬r, q, ¬p} Resolution between r∨p∨s and ¬s Resolution between p∨¬r and ¬p Resolution between r√p∨s and ¬p

## s₄ = {r∨p∨s, ¬p∨s, ¬s, p∨¬r, q, ¬p} Resolution between r∨p∨s and ¬s Resolution between p√¬r and ¬p Resolution between r√p∨s and ¬p

# $s_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$ Resolution between $r \lor p \lor s$ and $\neg s$ Resolution between $p \lor \neg r$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg p$

## $S_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$ Resolution between $r \lor p \lor s$ and $\neg s$ Resolution between $p \lor \neg r$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg p$ $\neg p \lor s$ can be subsumed into $\neg p$

$$s_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$$
  
Resolution between  $r \lor p \lor s$  and  $\neg s$   
Resolution between  $p \lor \neg r$  and  $\neg p$   
Resolution between  $r \lor p \lor s$  and  $\neg p$   
 $\neg p \lor s$  can be subsumed into  $\neg p$   
 $f_{wert,1}(\{\neg p, \neg p \lor s\}, \{\neg p\}) = 0$ 

Resolution between rvpvs and Resolution between pv¬r and ¬p Resolution between rvpvs and ¬p  $\neg p \lor s$  can be subsumed into  $\neg p$  $f_{wert,1}(\{\neg p, \neg p \lor s\}, \{\neg p\}) = 0$  $f_{wert,1}(\{p \lor \neg r, \neg p\}, \{p \lor \neg r, \neg p, \neg r\}) = 1$  $f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2$ 

 $s_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p \lor s \}$ Resolution between rvpvs and -Resolution between pv¬r and ¬p Resolution between rvpvs and ¬p ¬pvs can be subsumed into ¬p  $f_{wert,1}(\{\neg p, \neg p \lor s\}, \{\neg p\}) = 0$  $f_{wert,1}(\{p \lor \neg r, \neg p\}, \{p \lor \neg r, \neg p, \neg r\}) = 1$  $f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2$  $f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2$ 

$$\begin{split} s_4 &= \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p \} \\ \text{Resolution between } r \lor p \lor s \text{ and } \neg s \\ \text{Resolution between } p \lor \neg r \text{ and } \neg p \\ \text{Resolution between } r \lor p \lor s \text{ and } \neg p \\ \neg p \lor s \text{ can be subsumed into } \neg p \\ f_{wert,1}(\{\neg p, \neg p \lor s\}, \{\neg p\}) &= 0 \\ f_{wert,1}(\{p \lor \neg r, \neg p\}, \{p \lor \neg r, \neg p, \neg r\}) &= 1 \\ f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) &= 2 \\ f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) &= 2 \\ \end{split}$$

#### $S_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$

#### $S_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$

## $s_4 = \{r \lor p \lor s, \neg p \lor s, \neg s, p \lor \neg r, q, \neg p\}$

#### $S_5 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p\}$

## $s_5 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p\}$

## Resolution between r\p\s and ¬s Resolution between p\¬r and ¬p Resolution between r\p\s and ¬p

$$\begin{split} &f_{wert,1}(\{p \lor \neg r, \neg p\}, \{p \lor \neg r, \neg p, \neg r\}) = 1 \\ &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \end{split}$$

## $s_5 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p\}$

## Resolution between r\p\s and ¬s Resolution between p\¬r and ¬p Resolution between r\p\s and ¬p

$$\begin{aligned} &f_{wert,1}(\{p \lor \neg r, \neg p\}, \{p \lor \neg r, \neg p, \neg r\}) = 1 \\ &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \end{aligned}$$

#### $S_5 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p\}$

#### $S_5 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p\}$

# $S_5 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p\}$

#### $S_6 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p, \neg r\}$

#### $S_6 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p, \neg r\}$

#### Resolution between rvpvs and ¬s Resolution between rvpvs and ¬p

# $\begin{aligned} &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \end{aligned}$

$$S_6 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p, \neg r\}$$

#### Resolution between rvpvs and ¬s Resolution between rvpvs and ¬p

# $\begin{aligned} &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \end{aligned}$

$$S_6 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p, \neg r\}$$

#### Resolution between rvpvs and ¬s Resolution between rvpvs and ¬p

# $\begin{aligned} &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \end{aligned}$
$$S_6 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p, \neg r\}$$

#### Resolution between rvpvs and ¬s Resolution between rvpvs and ¬p

## $\begin{aligned} &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \end{aligned}$

$$S_6 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p, \neg r\}$$

Resolution between r\p\s and ¬s Resolution between r\p\s and ¬p p\¬r can be subsumed into ¬r

$$\begin{aligned} &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \end{aligned}$$

$$S_6 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p, \neg r\}$$

#### Resolution between r\p\s and ¬s Resolution between r\p\s and ¬p p\¬r can be subsumed into ¬r

$$\begin{aligned} &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \end{aligned}$$

$$S_6 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p, \neg r\}$$

#### Resolution between r\p\s and ¬s Resolution between r\p\s and ¬p p\¬r can be subsumed into ¬r

$$\begin{aligned} &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \end{aligned}$$

$$s_6 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p, \neg r\}$$
  
Resolution between  $r \lor p \lor s$  and  $\neg s$   
Resolution between  $r \lor p \lor s$  and  $\neg p$   
 $p \lor \neg r$  can be subsumed into  $\neg r$ 

$$\begin{aligned} &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \end{aligned}$$

$$\begin{aligned} &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \end{aligned}$$

$$\begin{split} f_{wert,1}(\{\neg r, p \lor \neg r\}, \{\neg r\}) &= 0 \\ f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) &= 2 \\ f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) &= 2 \end{split}$$

$$\begin{split} f_{wert,1}(\{\neg r, p \lor \neg r\}, \{\neg r\}) &= 0 \\ f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) &= 2 \\ f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) &= 2 \\ f_{wert,1}(\{r \lor p \lor s, \neg r\}, \{r \lor p \lor s, \neg r, p \lor s\}) &= 2 \end{split}$$

$$\begin{aligned} & f_{wert,1}(\{\neg r, p \lor \neg r\}, \{\neg r\}) = 0 \\ & f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ & f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \\ & f_{wert,1}(\{r \lor p \lor s, \neg r\}, \{r \lor p \lor s, \neg r, p \lor s\}) = 2 \end{aligned}$$

#### $S_6 = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p, \neg r\}$

## s<sub>6</sub> = {r∨p∨s, ¬s, p∨¬r, q, ¬p, ¬r}

# $s_{6} = \{r \lor p \lor s, \neg s, p \lor \neg r, q, \neg p, \neg r\}$ $\downarrow$ $s_{7} = \{r \lor p \lor s, \neg s, q, \neg p, \neg r\}$

#### $s_7 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r\}$

Resolution between r\p\s and ¬s Resolution between r\p\s and ¬p Resolution between r\p\s and ¬r

$$\begin{aligned} &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg r\}, \{r \lor p \lor s, \neg r, p \lor s\}) = 2 \end{aligned}$$

#### $s_7 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r\}$

Resolution between r\p\s and ¬s Resolution between r\p\s and ¬p Resolution between r\p\s and ¬r

$$\begin{split} &f_{wert,1}(\{r \lor p \lor s, \neg s\}, \{r \lor p \lor s, \neg s, r \lor p\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2 \\ &f_{wert,1}(\{r \lor p \lor s, \neg r\}, \{r \lor p \lor s, \neg r, p \lor s\}) = 2 \end{split}$$

#### $s_7 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r\}$

#### $S_7 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r\}$

## s<sub>7</sub> = {r∨p∨s, ¬s, q, ¬p, ¬r}

 $S_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ 

## $s_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between $r \lor p \lor s$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg r$

## $s_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between $r \lor p \lor s$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg r$

## $s_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$

#### Resolution between $r \lor p \lor s$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg r$

## $s_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between $r \lor p \lor s$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg r$

### $s_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between $r \lor p \lor s$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg r$ $r \lor p \lor s$ can be subsumed into $r \lor p$

## $s_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between $r \lor p \lor s$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg r$ $r \lor p \lor s$ can be subsumed into $r \lor p$

## $s_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between $r \lor p \lor s$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg r$ $r \lor p \lor s$ can be subsumed into $r \lor p$

## s<sub>8</sub> = {r∨p∨s, ¬s, q, ¬p, ¬r, r∨p} Resolution between r∨p∨s and ¬p Resolution between r∨p∨s and ¬r r∨p∨s can be subsumed into r∨p

## $s_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between $r \lor p \lor s$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg r$ $r \lor p \lor s$ can be subsumed into $r \lor p$ Resolution between $r \lor p$ and $\neg r \lor p$

## $s_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p \}$ Resolution between $r \lor p \lor s$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg r$ $r \lor p \lor s$ can be subsumed into $r \lor p$ Resolution between $r \lor p$ and $\neg r \lor p$

## $s_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p \}$ Resolution between $r \lor p \lor s$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg r$ $r \lor p \lor s$ can be subsumed into $r \lor p$ Resolution between $r \lor p$ and $\neg r \lor p$

## $s_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between $r \lor p \lor s$ and $\neg p$ Resolution between $r \lor p \lor s$ and $\neg r$ $r \lor p \lor s$ can be subsumed into $r \lor p$ Resolution between $r \lor p$ and $\neg p$

## $S_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between $r \vee p \vee s$ and Resolution between rvpvs and ¬r rvpvs can be subsumed into rvp Resolution between rvp and ¬p Resolution between rvp<sup>4</sup>and ¬r

## $S_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between rvpvs and Resolution between rvpvs and ¬r rvpvs can be subsumed into rvp Resolution between r√p and ¬p Resolution between r∨p<sup>4</sup>and ¬r

 $f_{wert,1}(\{r \lor p \lor s, r \lor p\}, \{r \lor p\}) = 0$ 

## $S_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between rvpvs and -Resolution between rvpvs and ¬r rvpvs can be subsumed into rvp Resolution between r√p and ¬p Resolution between r∨p<sup>4</sup> and ¬r

 $f_{wert,1}(\{r \lor p \lor s, r \lor p\}, \{r \lor p\}) = 0$  $f_{wert,1}(\{r \lor p, \neg p\}, \{r \lor p, \neg p, r\}) = 1$ 

## $S_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between rvpvs and -p Resolution between rvpvs and ¬r rvpvs can be subsumed into rvp Resolution between r√p and ¬p Resolution between r∨p<sup>4</sup> and ¬r

$$\begin{split} &f_{wert,1}(\{r \lor p \lor s, r \lor p\}, \{r \lor p\}) = 0 \\ &f_{wert,1}(\{r \lor p, \neg p\}, \{r \lor p, \neg p, r\}) = 1 \\ &f_{wert,1}(\{r \lor p, \neg r\}, \{r \lor p, \neg r, p\}) = 1 \end{split}$$

## $S_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$ Resolution between rvpvs and -Resolution between rvpvs and ¬r rvpvs can be subsumed into rvp Resolution between r√p and ¬p Resolution between $r \vee p^{\prime}$ and $\neg r$

$$\begin{split} &f_{wert,1}(\{r \lor p \lor s, r \lor p\}, \{r \lor p\}) = 0 \\ &f_{wert,1}(\{r \lor p, \neg p\}, \{r \lor p, \neg p, r\}) = 1 \\ &f_{wert,1}(\{r \lor p, \neg r\}, \{r \lor p, \neg r, p\}) = 1 \end{split}$$

#### $S_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$

#### $S_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$
#### $S_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$

#### S<sub>9</sub> = {¬S, q, ¬p, ¬r, r∨p}

#### $S_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$

#### S<sub>9</sub> = {¬S, q, ¬p, ¬r, r∨p}

 $f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) = 2$ 

## S<sub>8</sub> = {r∨p∨s, ¬s, q, ¬p, ¬r, r∨p}

#### S<sub>9</sub> = {¬S, q, ¬p, ¬r, r∨p}

 $\begin{aligned} f_{wert,1}(\{r \lor p \lor s, \neg p\}, \{r \lor p \lor s, \neg p, r \lor s\}) &= 2 \\ f_{wert,1}(\{r \lor p \lor s, \neg r\}, \{r \lor p \lor s, \neg r, p \lor s\}) &= 2 \end{aligned}$ 

#### $S_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$

#### S<sub>9</sub> = {¬S, q, ¬p, ¬r, r∨p}

 $f_{wert,1}(\{r \lor p \lor s, \neg r\}, \{r \lor p \lor s, \neg r, p \lor s\}) = 2$ 

#### $S_8 = \{r \lor p \lor s, \neg s, q, \neg p, \neg r, r \lor p\}$

#### S<sub>9</sub> = {¬S, q, ¬p, ¬r, r∨p}

#### s<sub>9</sub> = {¬s, q, ¬p, ¬r, r∨p} Resolution between r∨p and ¬p Resolution between r∨p and ¬r

## $\begin{aligned} f_{wert,1}(\{r \lor p, \neg p\}, \{r \lor p, \neg p, r\}) &= 1 \\ f_{wert,1}(\{r \lor p, \neg r\}, \{r \lor p, \neg r, p\}) &= 1 \end{aligned}$

#### s<sub>9</sub> = {¬s, q, ¬p, ¬r, r∨p} Resolution between r∨p and ¬p Resolution between r∨p and ¬r

 $\begin{aligned} f_{wert,1}(\{r \lor p, \neg p\}, \{r \lor p, \neg p, r\}) &= 1 \\ f_{wert,1}(\{r \lor p, \neg r\}, \{r \lor p, \neg r, p\}) &= 1 \end{aligned}$ 

#### $S_9 = \{\neg S, q, \neg p, \neg r, r \lor p\}$

#### $S_9 = \{\neg S, q, \neg p, \neg r, r \lor p\}$

## S<sub>9</sub> = {¬S, q, ¬p, ¬r, r∨p} ↓ S<sub>10</sub> = {¬S, q, ¬p, ¬r, r∨p, r}

s<sub>10</sub> = {¬s, q, ¬p, ¬r, r∨p, r} Resolution between r∨p and ¬p Resolution between r∨p and ¬r

#### $s_{10} = \{\neg s, q, \neg p, \neg r, r \lor p, r\}$ Resolution between r\p and $\neg p$ Resolution between r\p and $\neg r$

#### $s_{10} = \{\neg s, q, \neg p, \neg r, r \lor p, r\}$ Resolution between $r \lor p$ and $\neg p$ Resolution between $r \lor p$ and $\neg r$

#### $s_{10} = \{\neg s, q, \neg p, \neg r, r \lor p, r\}$ Resolution between $r \lor p$ and $\neg p$ Resolution between $r \lor p$ and $\neg r$

#### s<sub>10</sub> = {¬s, q, ¬p, ¬r, r∨p, r} Resolution between r∨p and ¬p Resolution between r∨p and ¬r Resolution between r and ¬r

#### s<sub>10</sub> = {¬s, q, ¬p, ¬r, r∨p, r} Resolution between r∨p and ¬p Resolution between r∨p and ¬r Resolution between r and ¬r

#### s<sub>10</sub> = {¬s, q, ¬p, ¬r, r∨p, r} Resolution between r∨p and ¬p Resolution between r∨p and ¬r Resolution between r and ¬r

#### $s_{10} = \{\neg s, q, \neg p, \neg r, r \lor p, r\}$ Resolution between r\p and \p Resolution between r\p and \ggr r Resolution between r \p and \ggr r

#### S<sub>10</sub> = {¬S, q, ¬p, ¬r, r∨p, r Resolution between r∨p and ¬p Resolution between r∨p and ¬r Resolution between r and ¬r r∨p can be subsumed into r

# S10 = {¬s, q, ¬p, ¬r, r∨p, r} Resolution between r∨p and ¬p Resolution between r∨p and ¬r Resolution between r and ¬r ryp can be subsumed into r

### f<sub>wert,1</sub>({¬r, r}, {□}) = 0

#### $s_{10} = \{\neg s, q, \neg p, \neg r, r \lor p, r\}$ Resolution between r\p and \p Resolution between r\p and \ggamma r Resolution between r\p and \ggamma r r\p can be subsumed into r

## $$\begin{split} f_{wert,1}(\{\neg r, r\}, \{ [ ] \}) &= 0\\ f_{wert,1}(\{r \lor p, r\}, \{r\}) &= 0\\ f_{wert,1}(\{r \lor p, \neg r\}, \{r \lor p, \neg r, p\}) &= 1 \end{split}$$

#### S<sub>10</sub> = {¬S, q, ¬p, ¬r, r∨p, r} Resolution between r∨p and ¬p Resolution between r∨p and ¬r Resolution between r and ¬r r∨p can be subsumed into r

$$\begin{split} f_{wert,1}(\{\neg r, r\}, \{ ] \}) &= 0 \\ f_{wert,1}(\{r \lor p, r\}, \{r\}) &= 0 \\ f_{wert,1}(\{r \lor p, \neg r\}, \{r \lor p, \neg r, p\}) &= 1 \end{split}$$

#### $s_{10} = \{\neg s, q, \neg p, \neg r, r \lor p, r\}$

#### s<sub>10</sub> = {¬s, q, ¬p, ¬r, r∨p, r}

## $s_{10} = \{\neg s, q, \neg p, \neg r, r \lor p, r\}$ $\downarrow$ $s_{11} = \{\neg s, q, \neg p, \neg r, r \lor p, r, []\}$

#### s<sub>11</sub> = {¬s, q, ¬p, ¬r, r∨p, r, □}

#### s<sub>11</sub> = {¬s, q, ¬p, ¬r, r∨p, r, □}

 $G(s_{11}) = yes$